



Aspects of Graphene Nanoribbons Devices Simulations

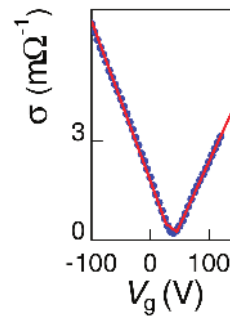
Pedro Brandimarte

June 13, 2016



Graphene

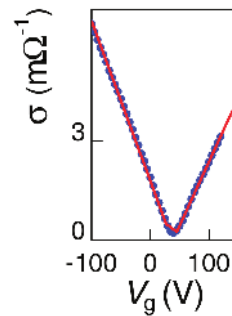
- High mobility $\rightarrow 10^5 \text{ cm}^2\text{V}^{-1}\text{s}^{-1}$



K. Novoselov et al. *Science* **306**, 666-669 (2004).

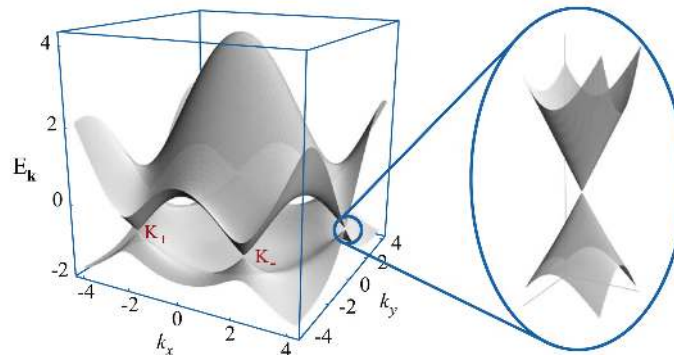
Graphene

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K. Novoselov *et al.* *Science* **306**, 666-669 (2004).

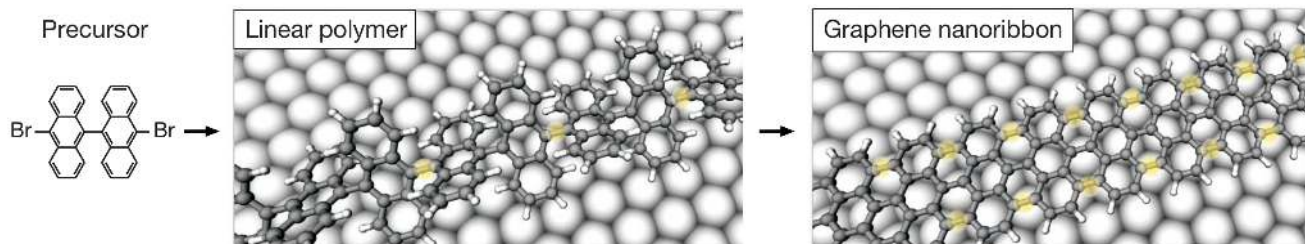
- Gap absence:



A. Castro Neto *et al.* *Rev. of Mod. Phys.* **81**, 109-162 (2009).

Graphene Nanoribbons (GNRs)

- Bottom-up fabrication of both AGNR and ZGNR by on-surface reaction of molecular precursors.

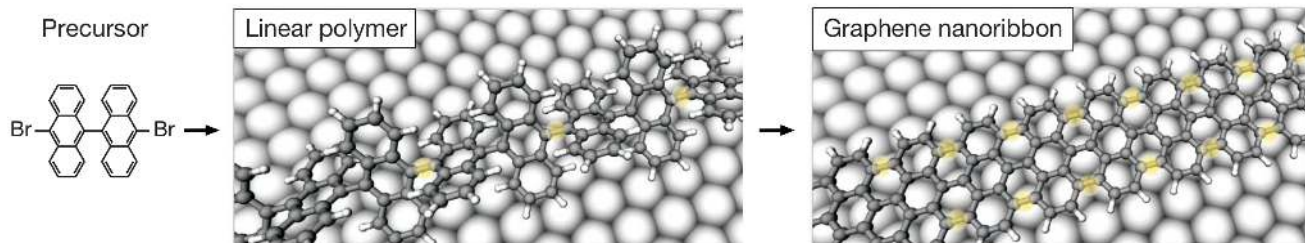


J. Cai *et al.* *Nature* **466**, 470 (2010).

L. Talirz, P. Ruffieux, and R. Fasel. *Advanced Materials* (2016).

Graphene Nanoribbons (GNRs)

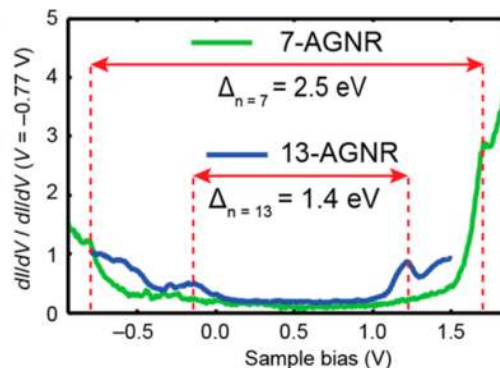
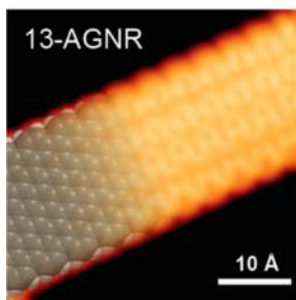
- Bottom-up fabrication of both AGNR and ZGNR by on-surface reaction of molecular precursors.



J. Cai *et al.* *Nature* **466**, 470 (2010).

L. Talirz, P. Ruffieux, and R. Fasel. *Advanced Materials* (2016).

- Semiconductor character, with energy gap depending on their width and shape.



Y.-W. Son *et al.* *Phys. Rev. Lett.* **97**, 216803 (2006).

Y.-C. Chen *et al.* *ACS Nano* **7**, 6123 (2013).

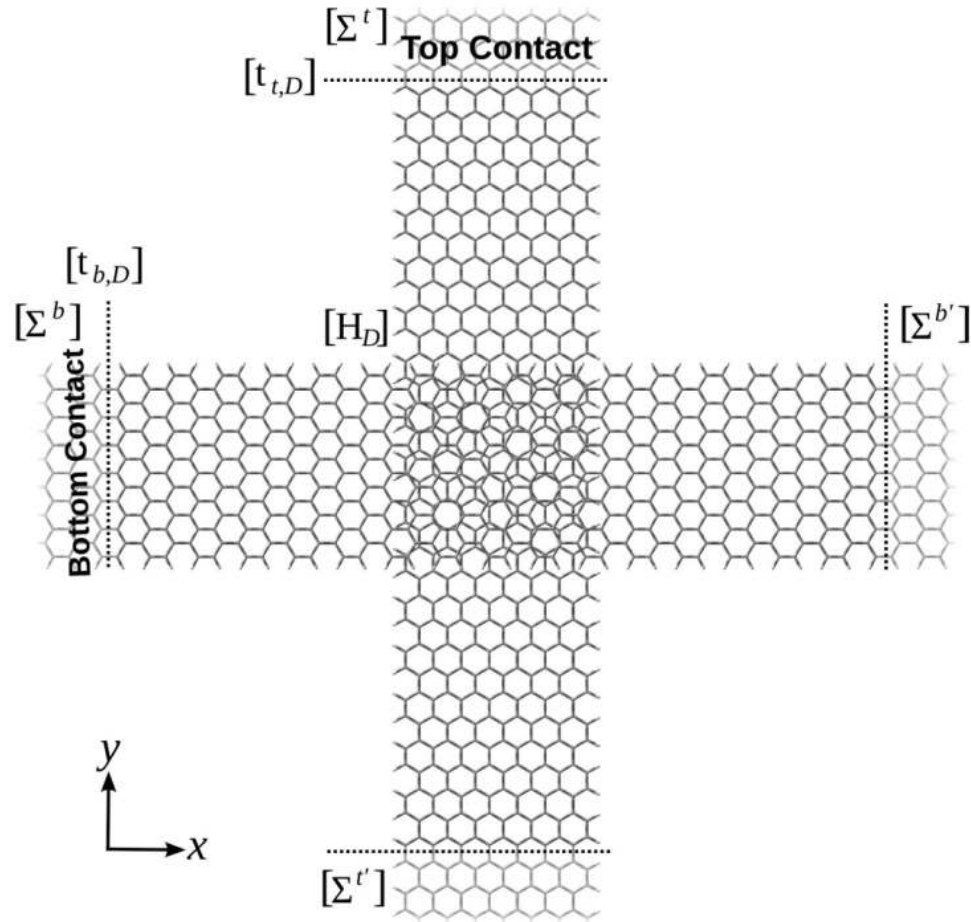
A. Kimouche *et al.* *Nature Communications* **6**, 10177 (2015).



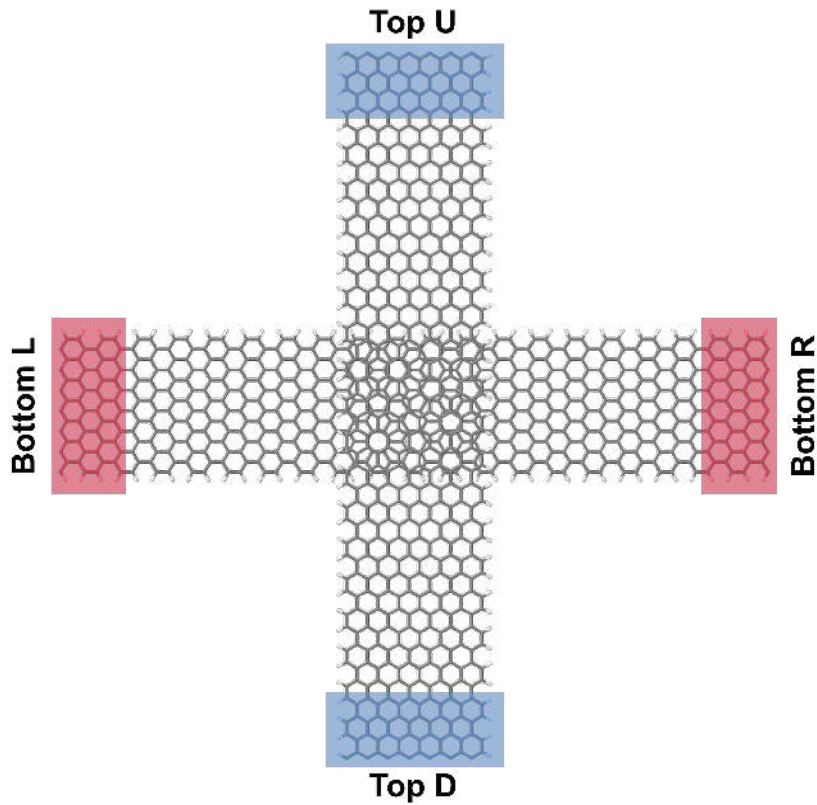
Electron Transport Simulations of 4-Terminal Crossed Graphene Nanoribbons Devices

Pedro Brandimarte, Nick R. Papior, Mads Engelund,
Aran Garcia-Lekue, Thomas Frederiksen, and Daniel Sánchez-Portal

June 13, 2016



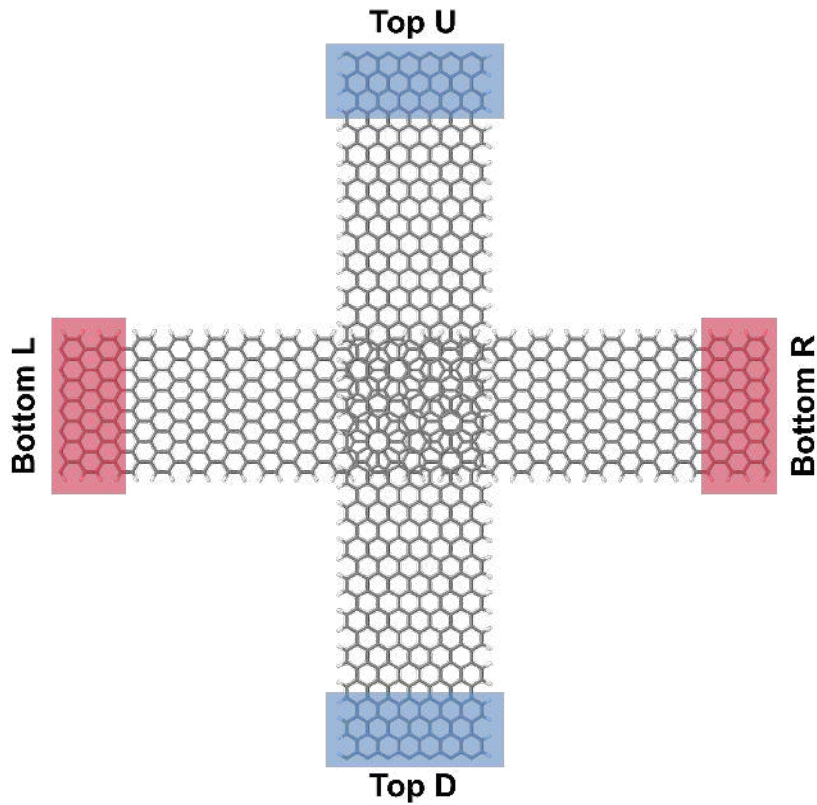
Crossed 14-AGNR



Density-Functional Theory (DFT)
+
Non-Equilibrium Green's Function (NEGF)

TranSIESTA

Crossed 14-AGNR



Density-Functional Theory (DFT)
+
Non-Equilibrium Green's Function (NEGF)

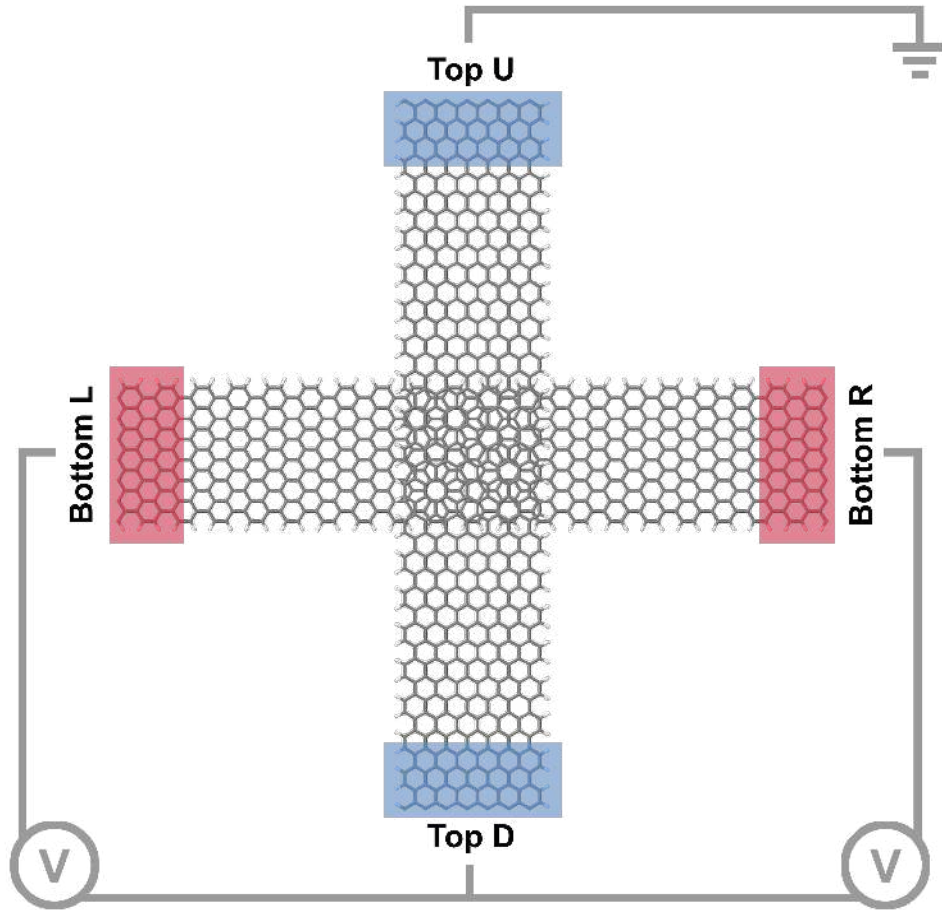
TranSIESTA

J. M. Soler *et al.* *J. Phys. Condens. Matter.* **14**, 2745 (2002).

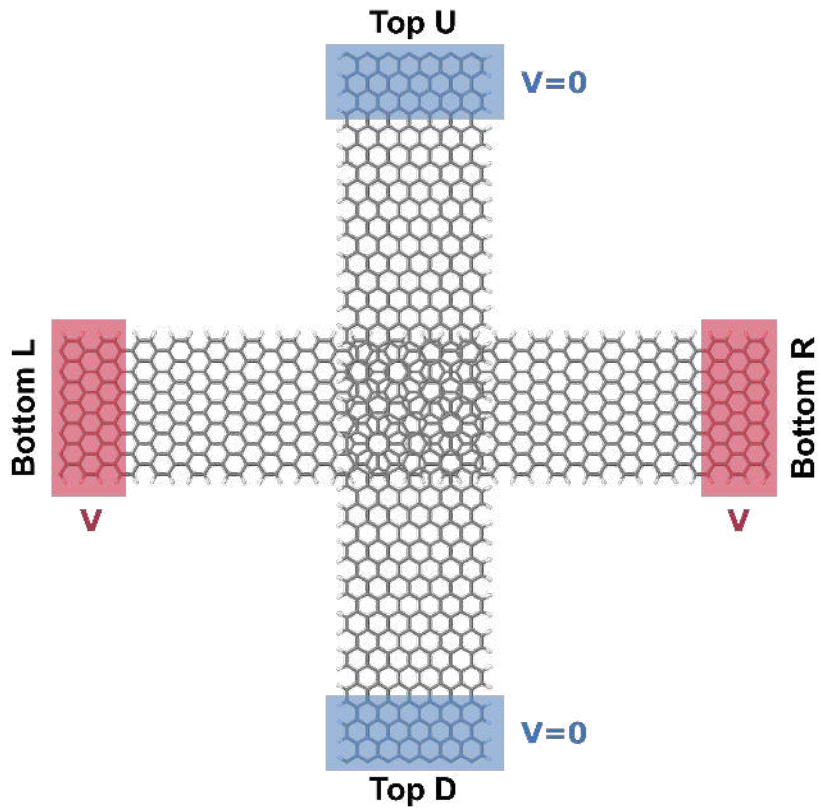
Mads Brandbyge *et al.* *Phys. Rev. B* **65**, 165401 (2002).

Nick R. Papior. *In preparation* (2016).

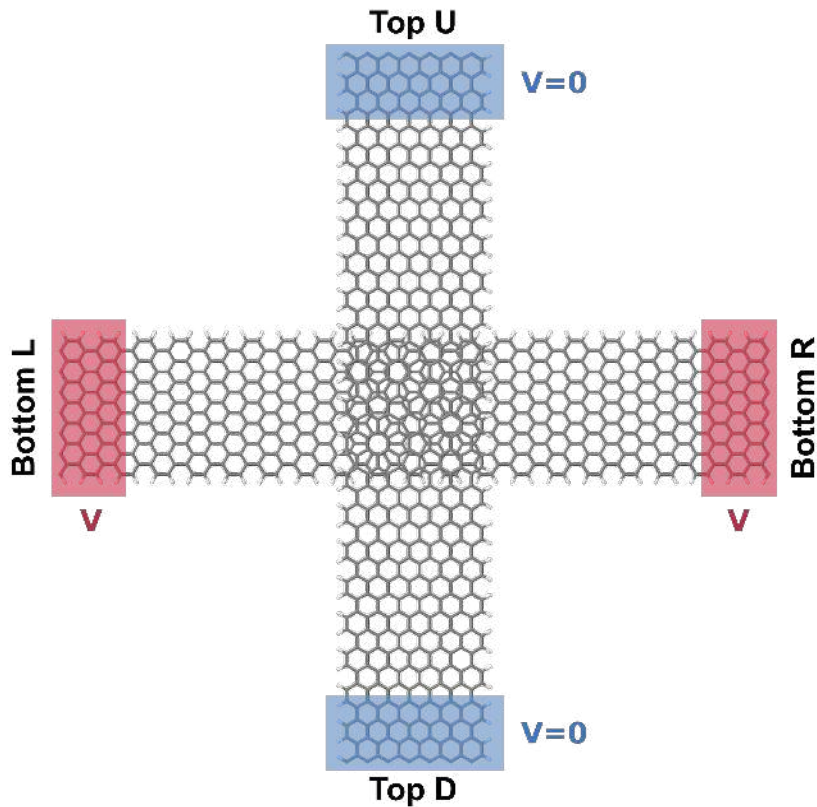
Crossed 14-AGNR



Crossed 14-AGNR



Crossed 14-AGNR

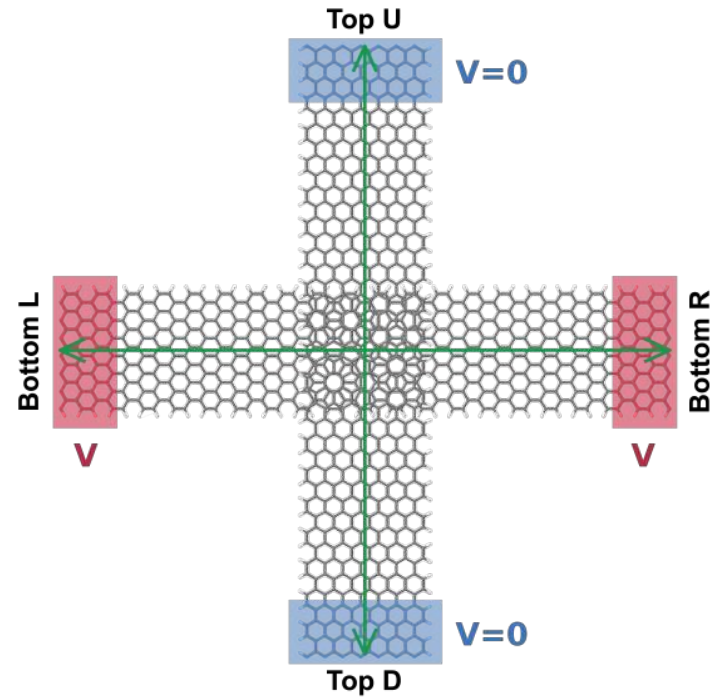
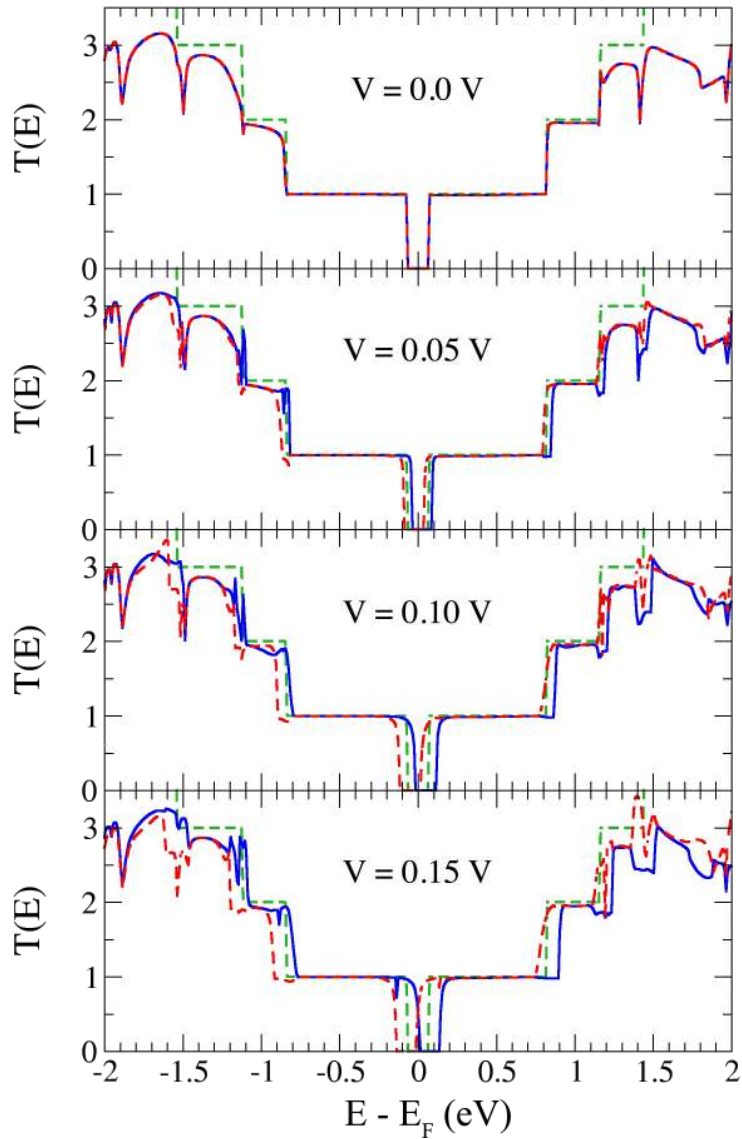


Simulation characteristics:

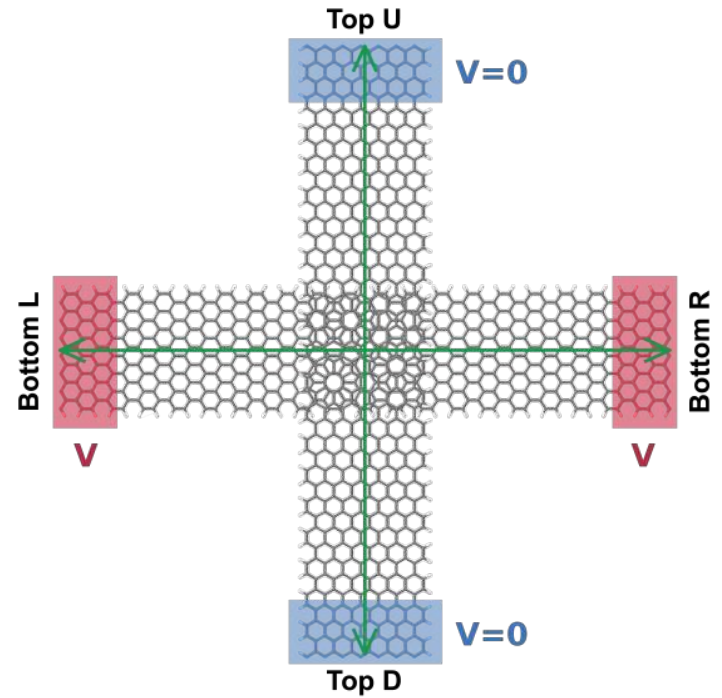
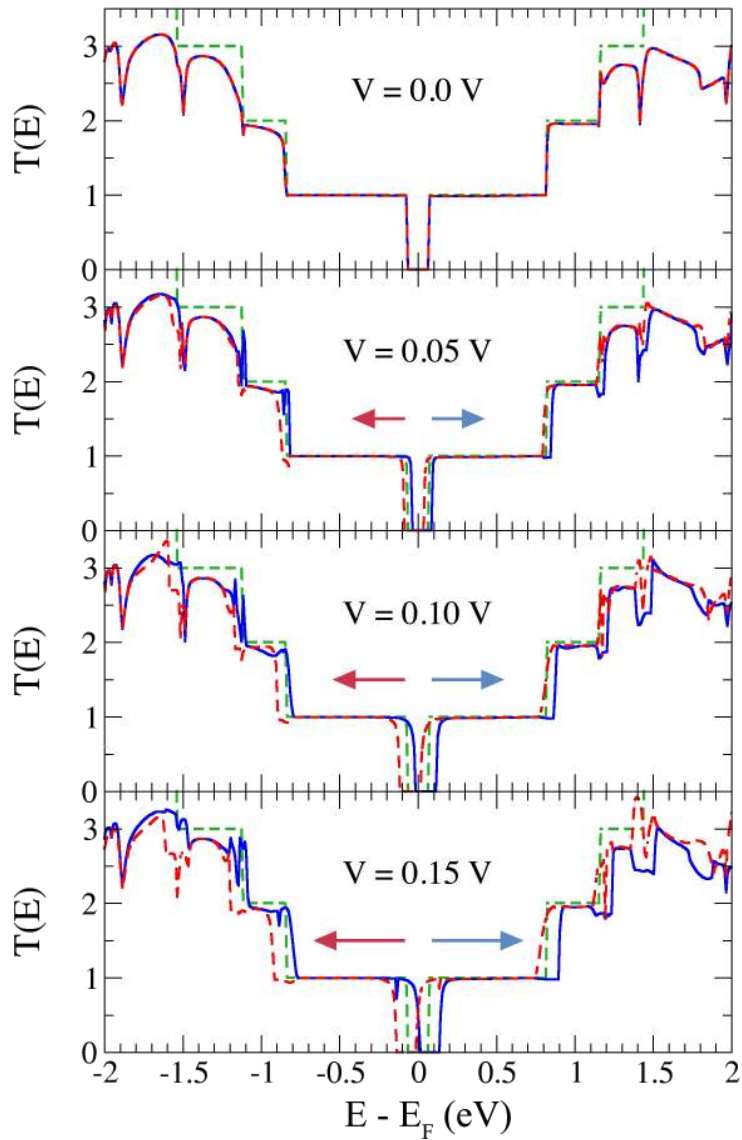
- 1280 atoms;
- double- ζ (9280 orbitals);
- vdW (optB88);
- real space grid cutoff: 350 Ry;
- forces < 5 meV/Å;
- interlayer distance: 3.34 Å.



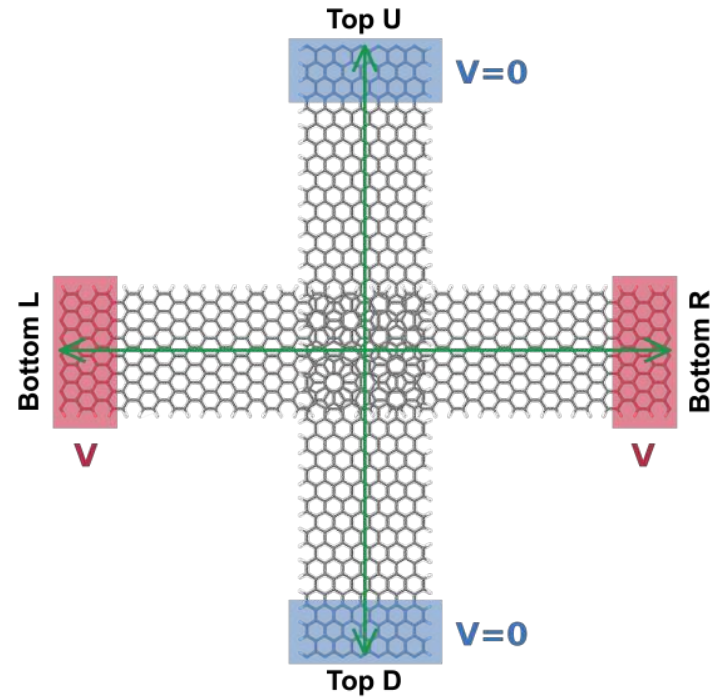
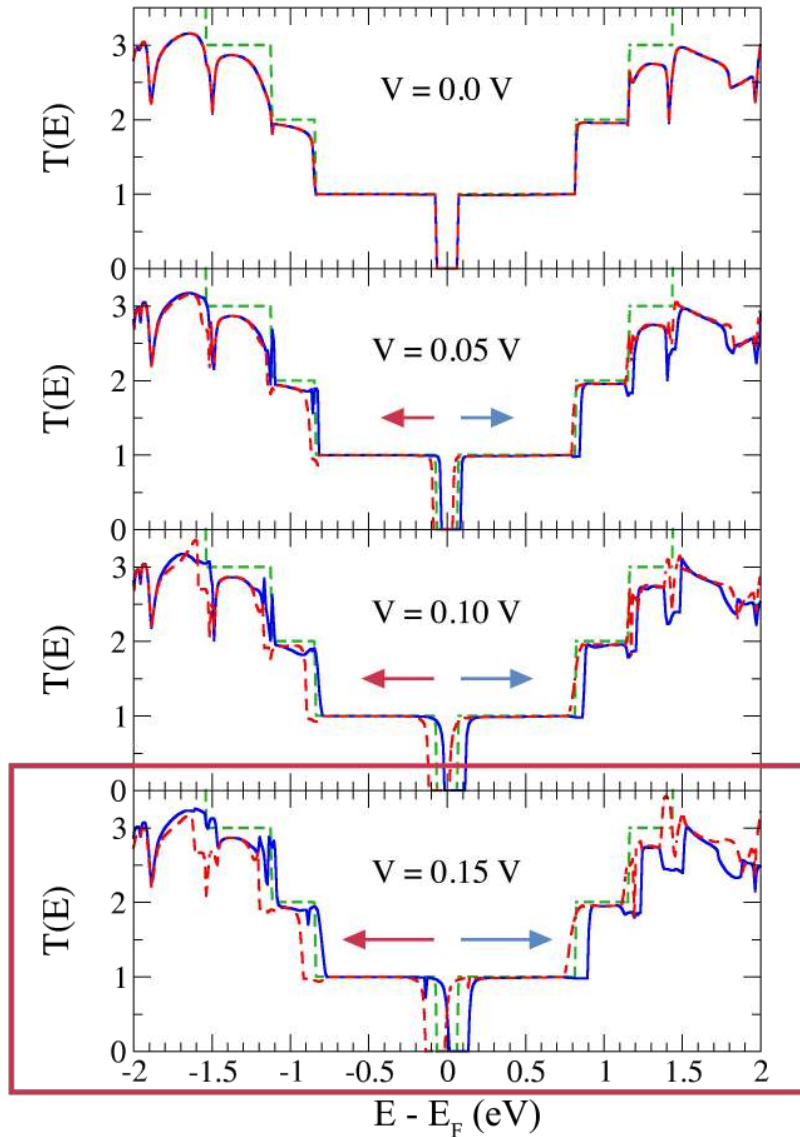
Direct transmission



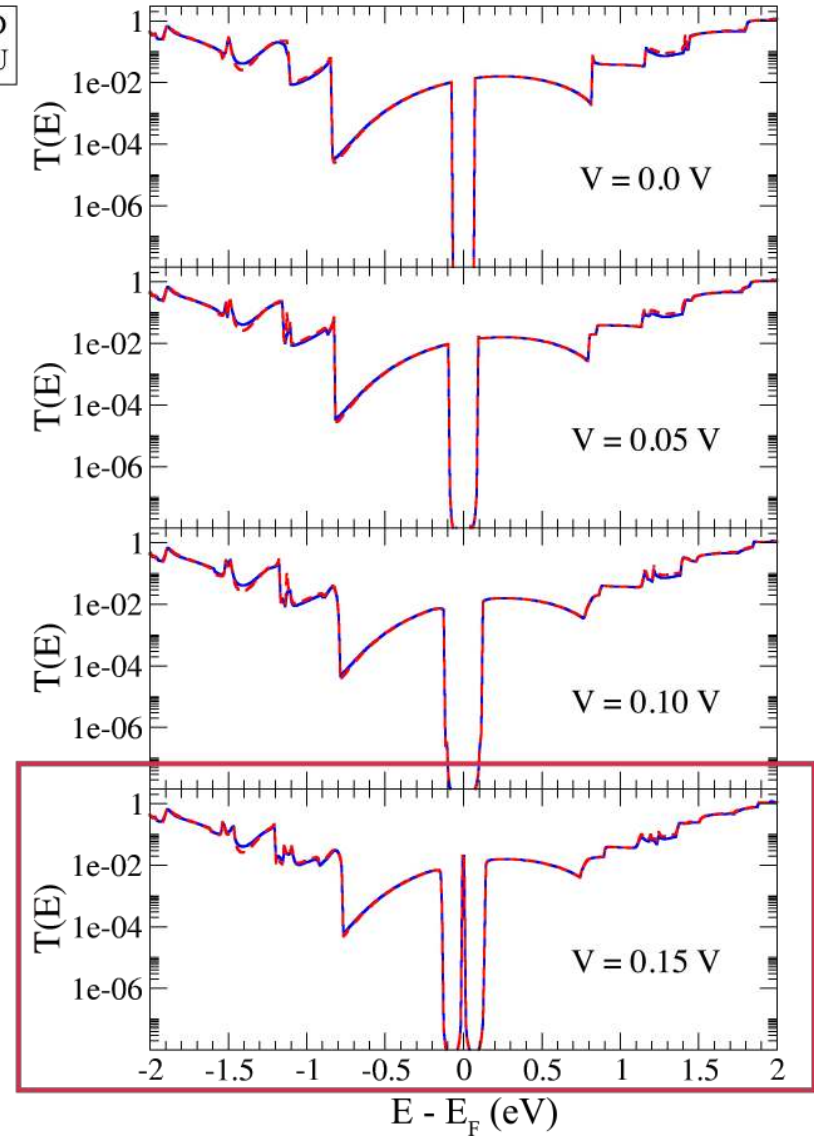
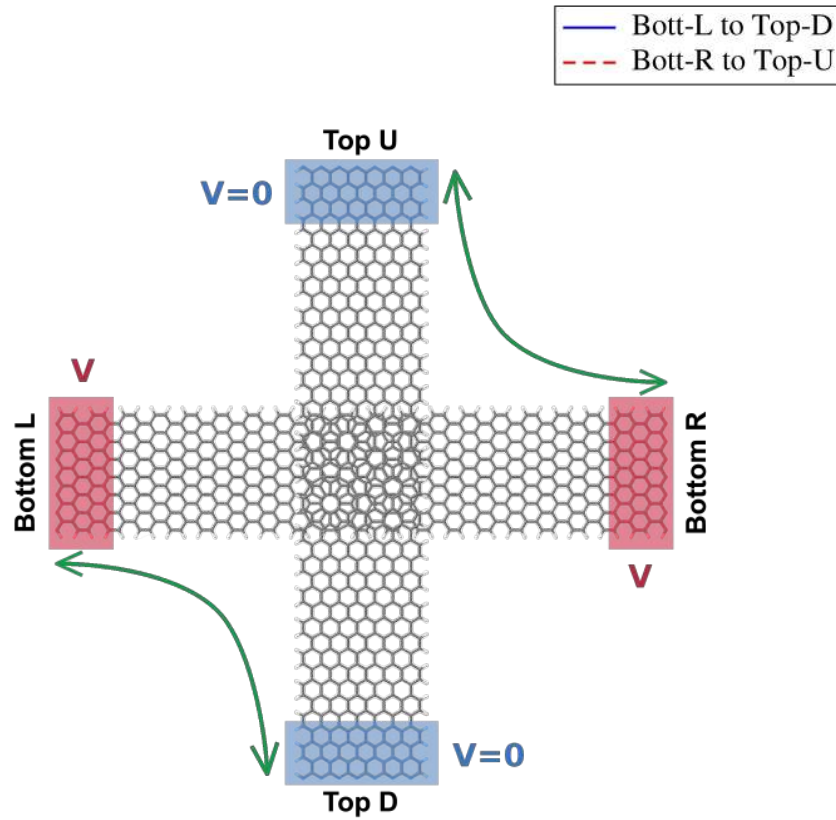
Direct transmission



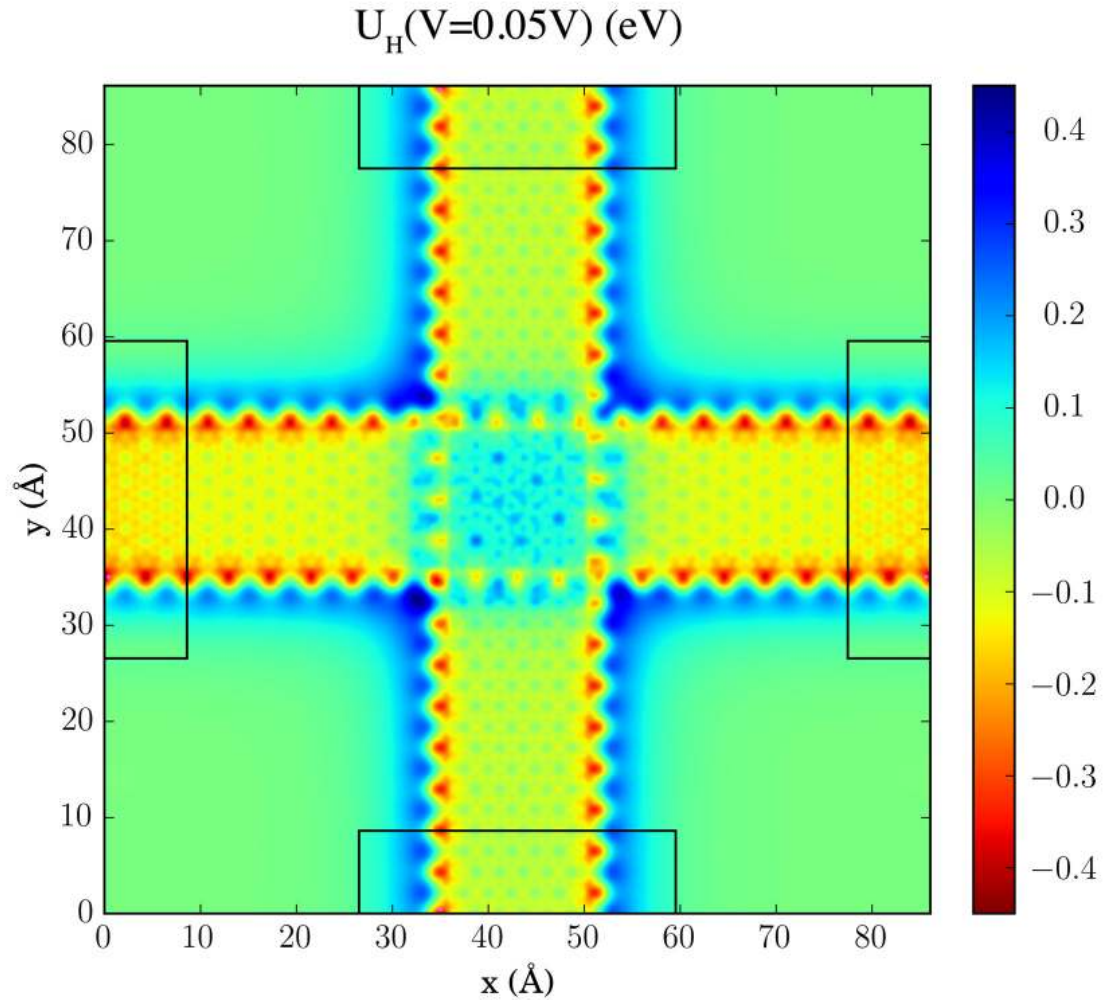
Direct transmission



Inter-ribbon transmission

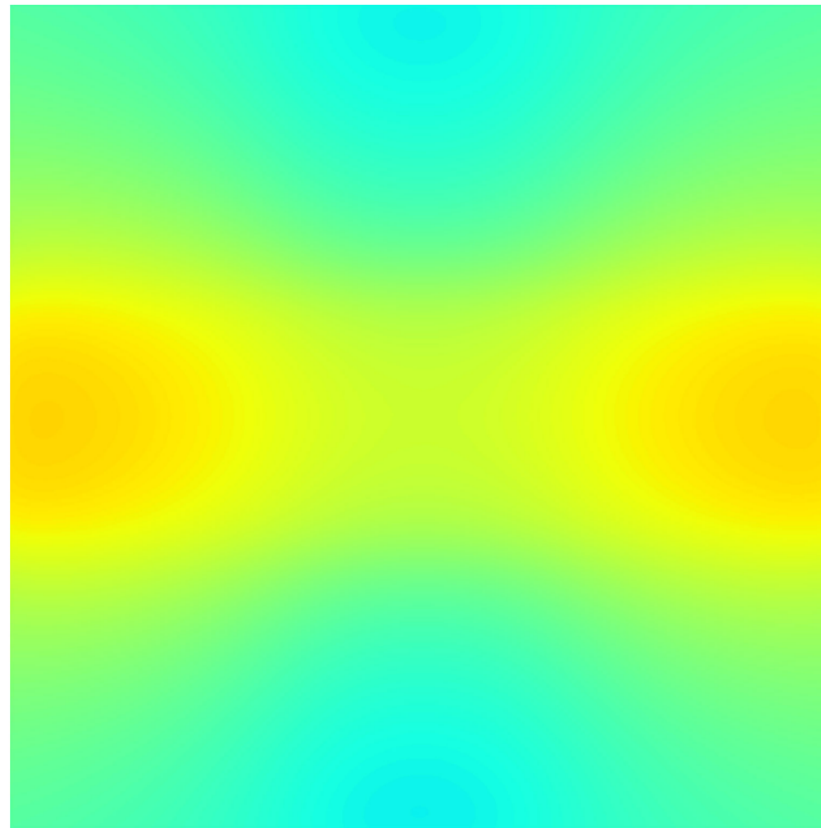


Electrostatic potential at 0.05 V



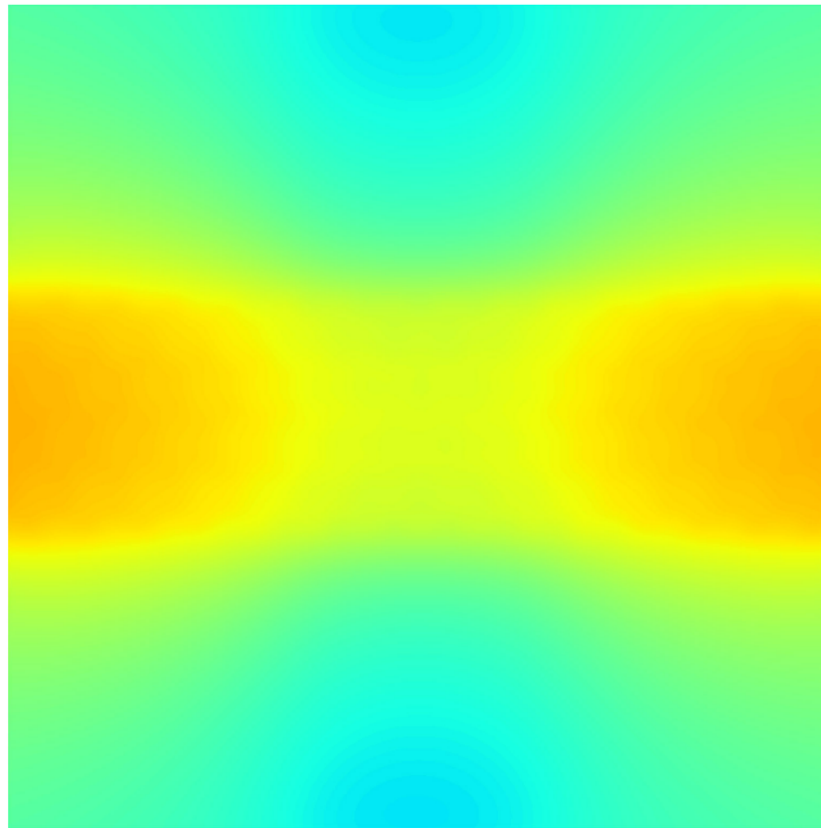
Electrostatic potential at 0.05 V

$$U_H(V=0.05V) - U_H(V=0.0V) \text{ (eV)}$$



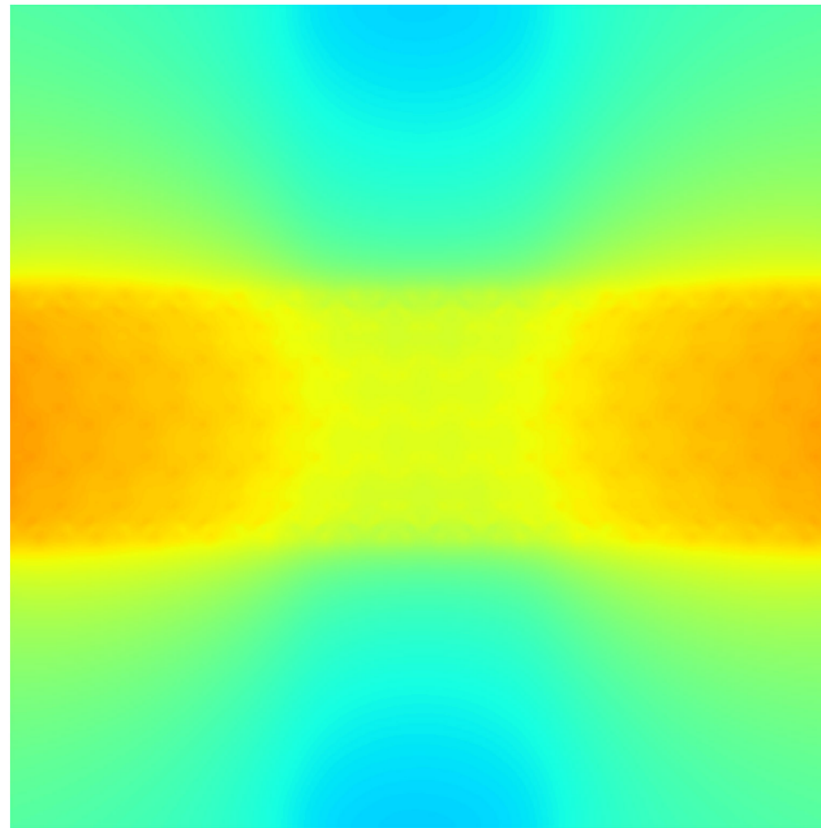
Electrostatic potential at 0.05 V

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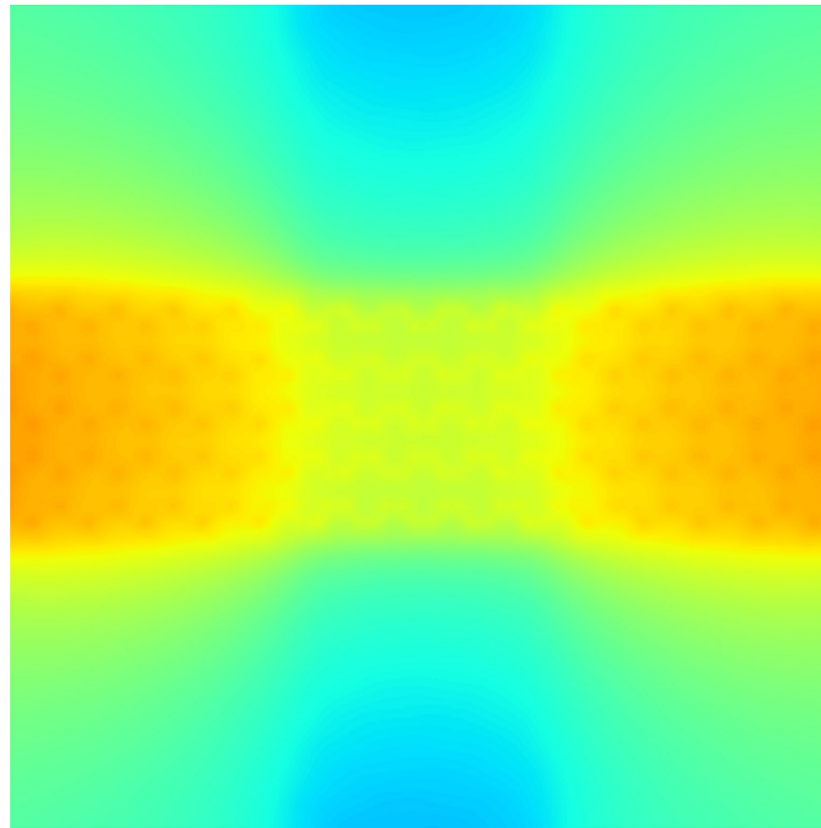
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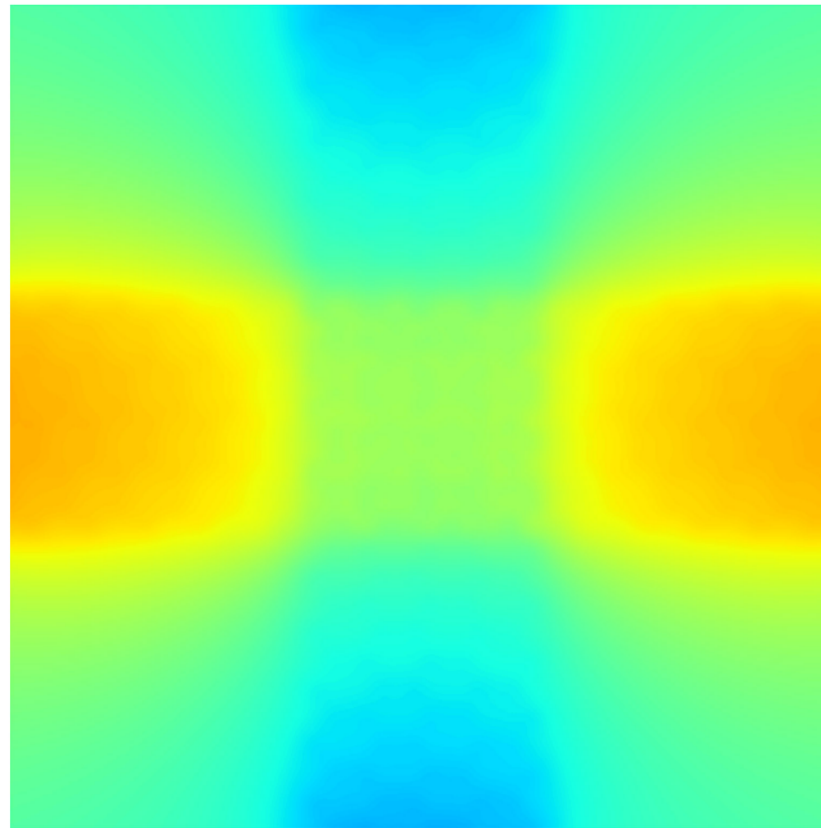
Electrostatic potential at 0.05 V

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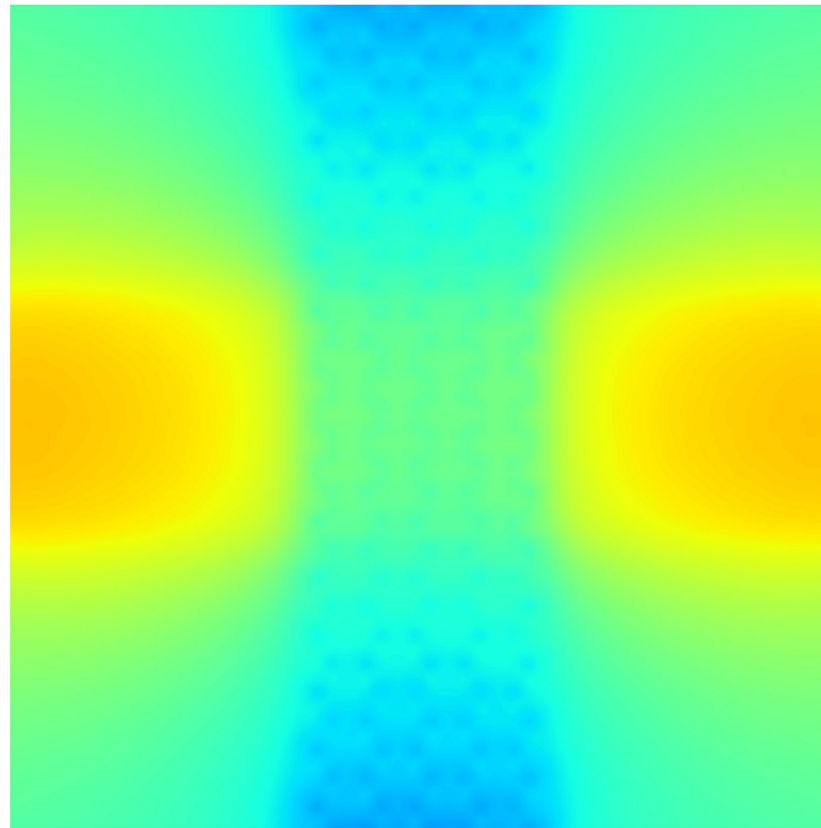
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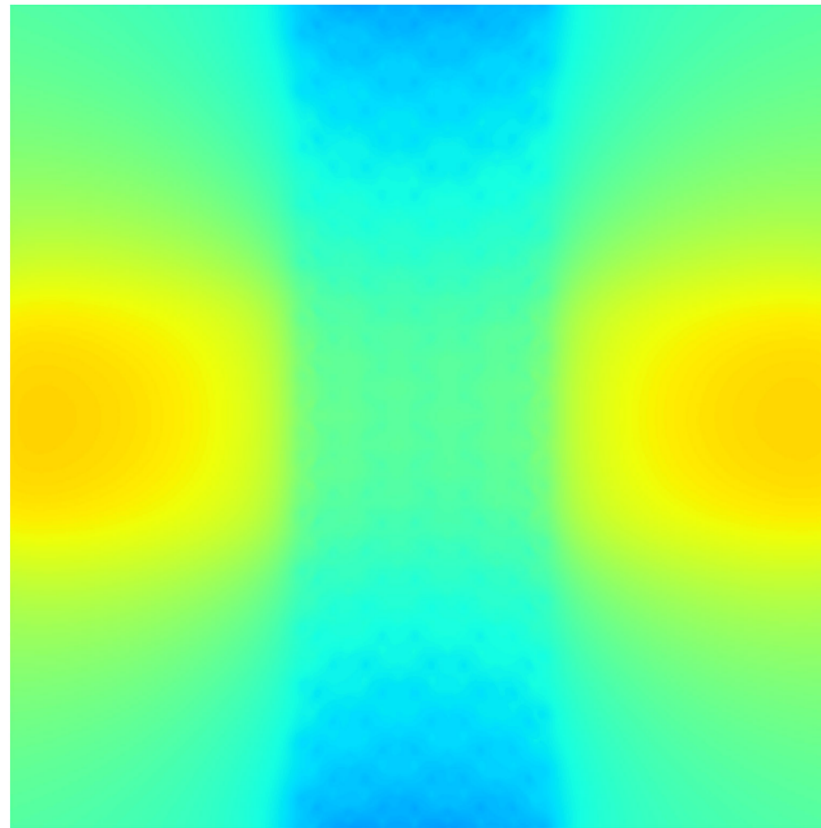
Electrostatic potential at 0.05 V

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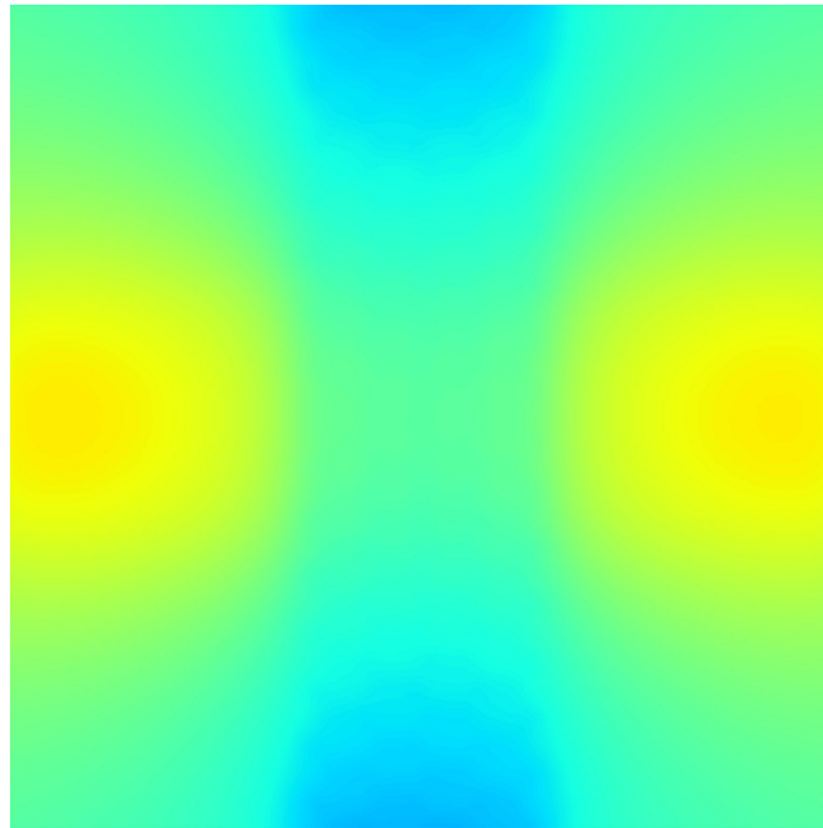
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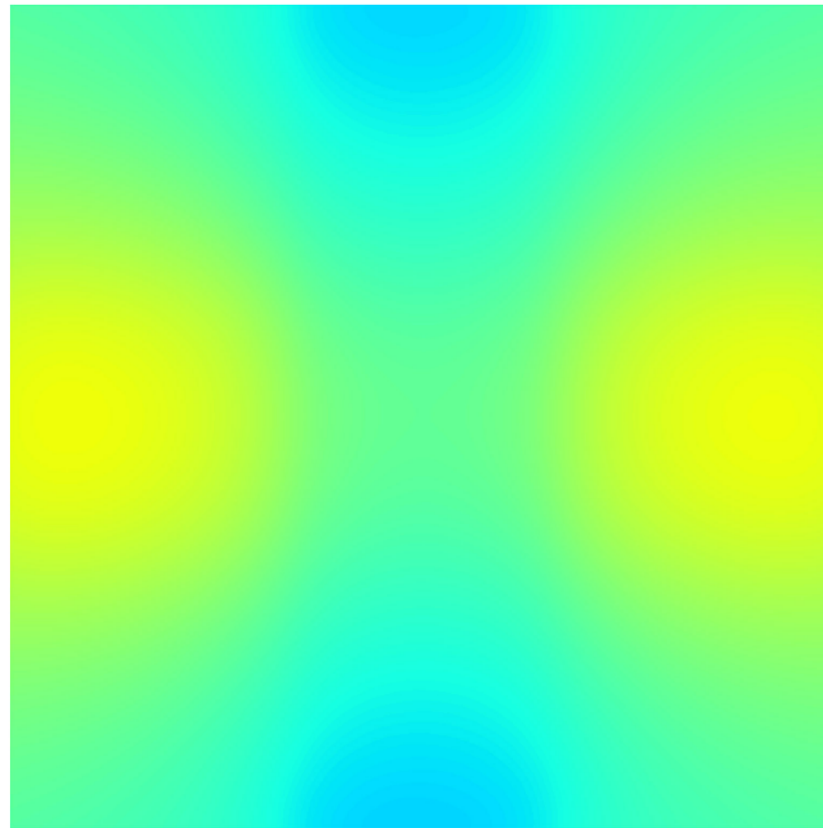
Electrostatic potential at 0.05 V

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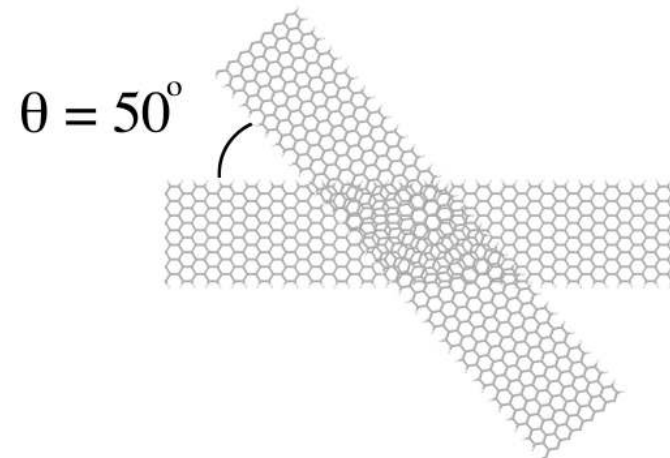
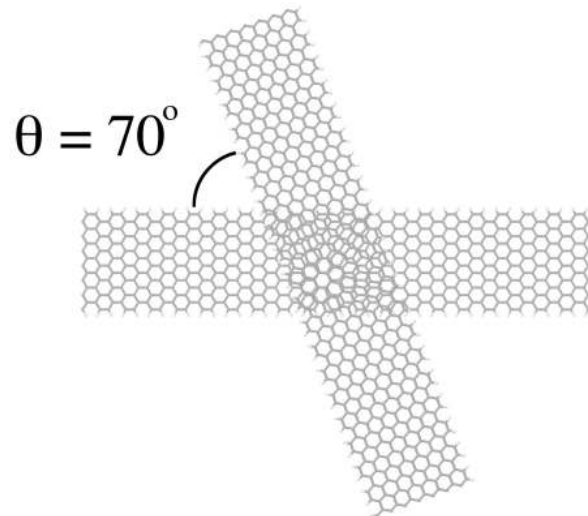
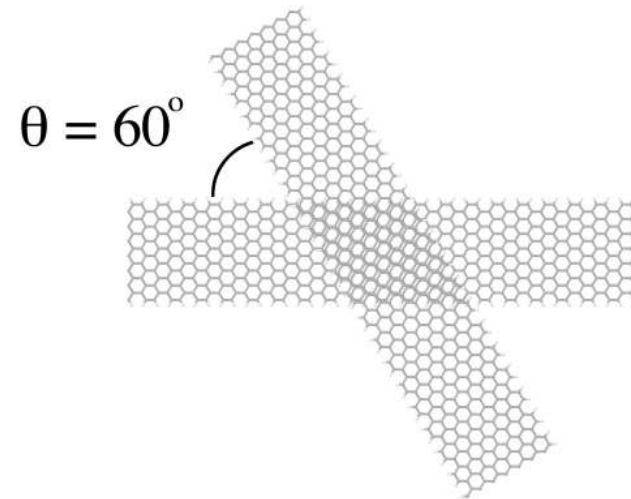
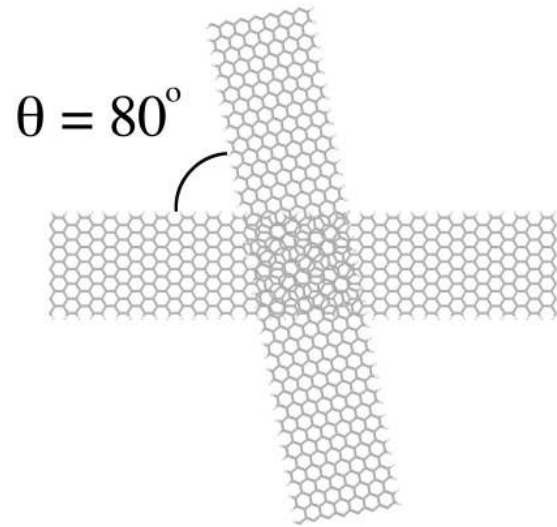


Electrostatic potential at 0.05 V

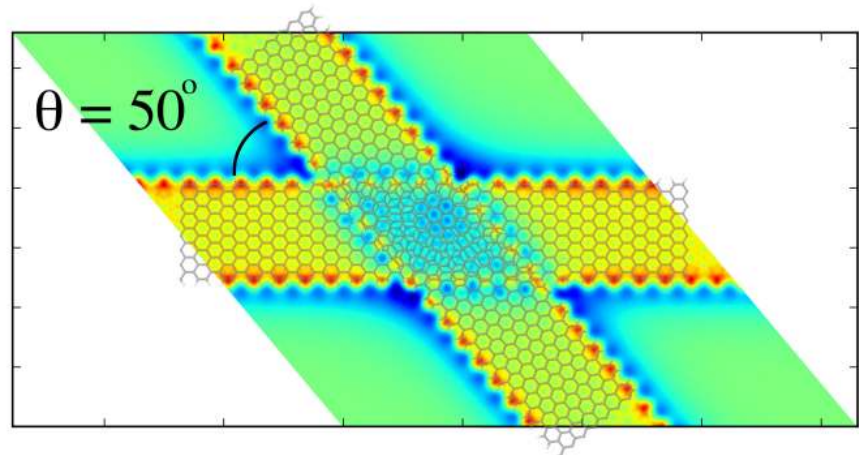
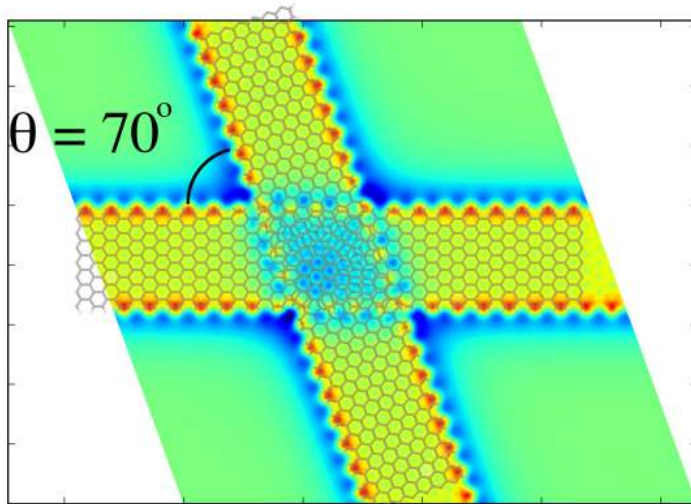
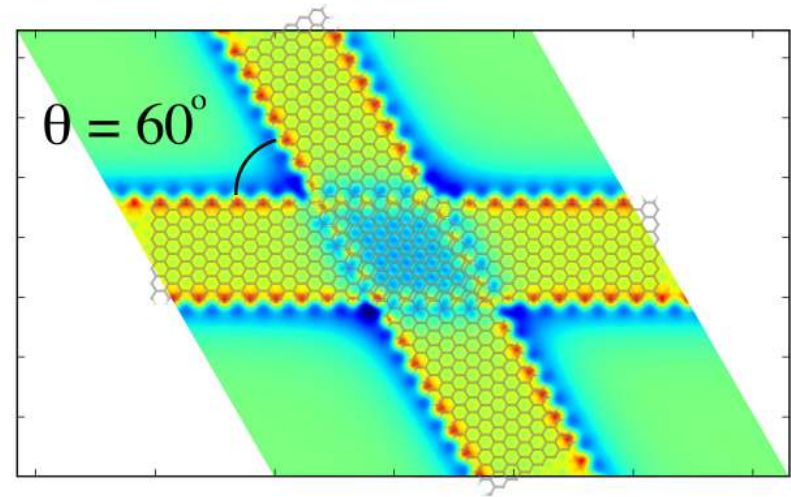
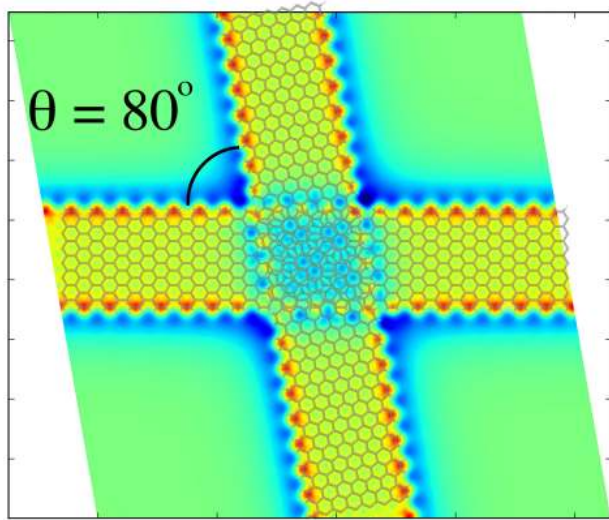
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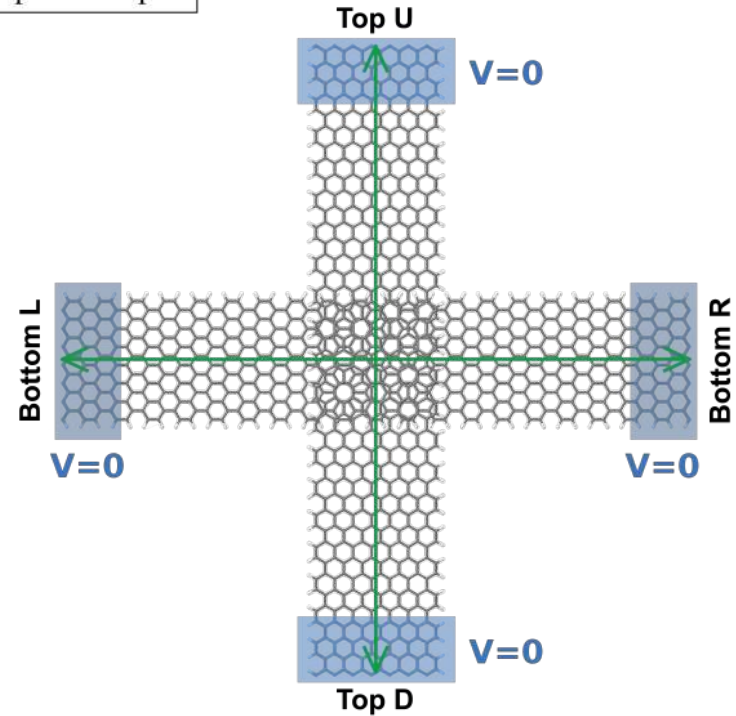
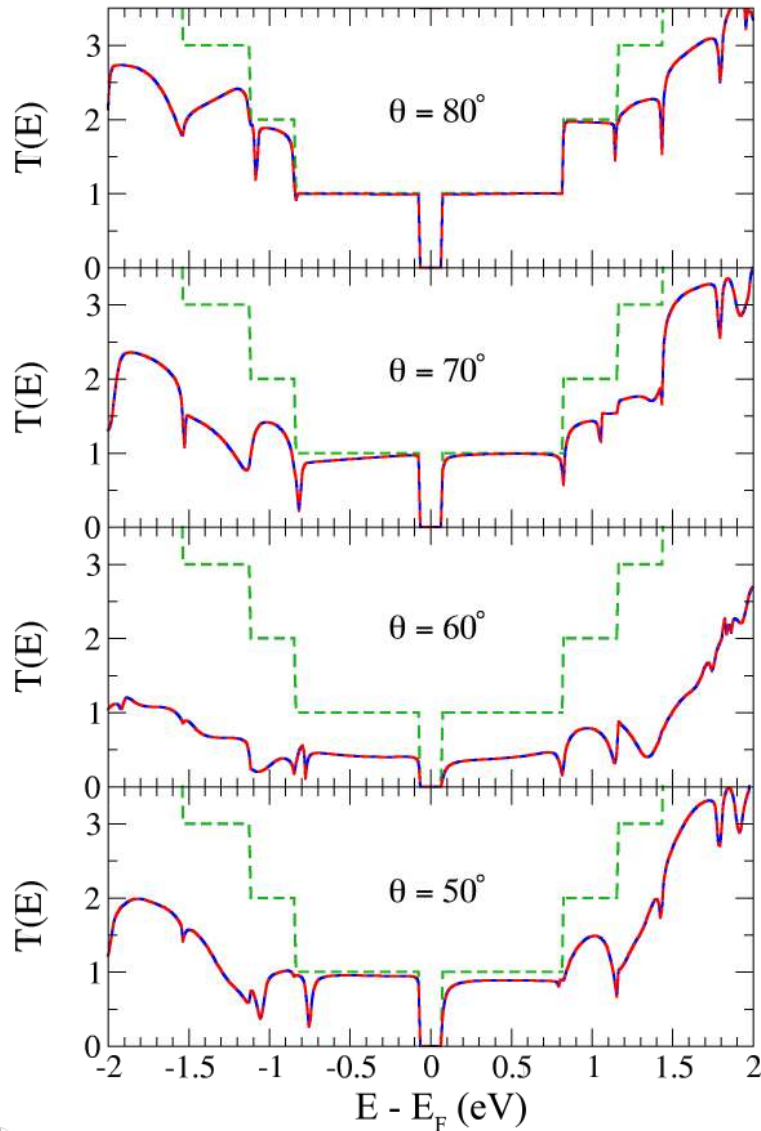
Rotated crossbar



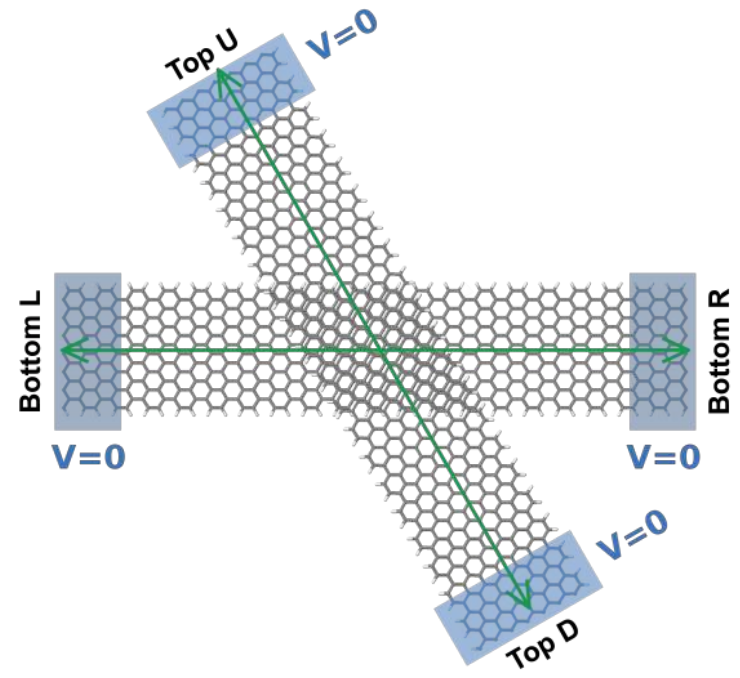
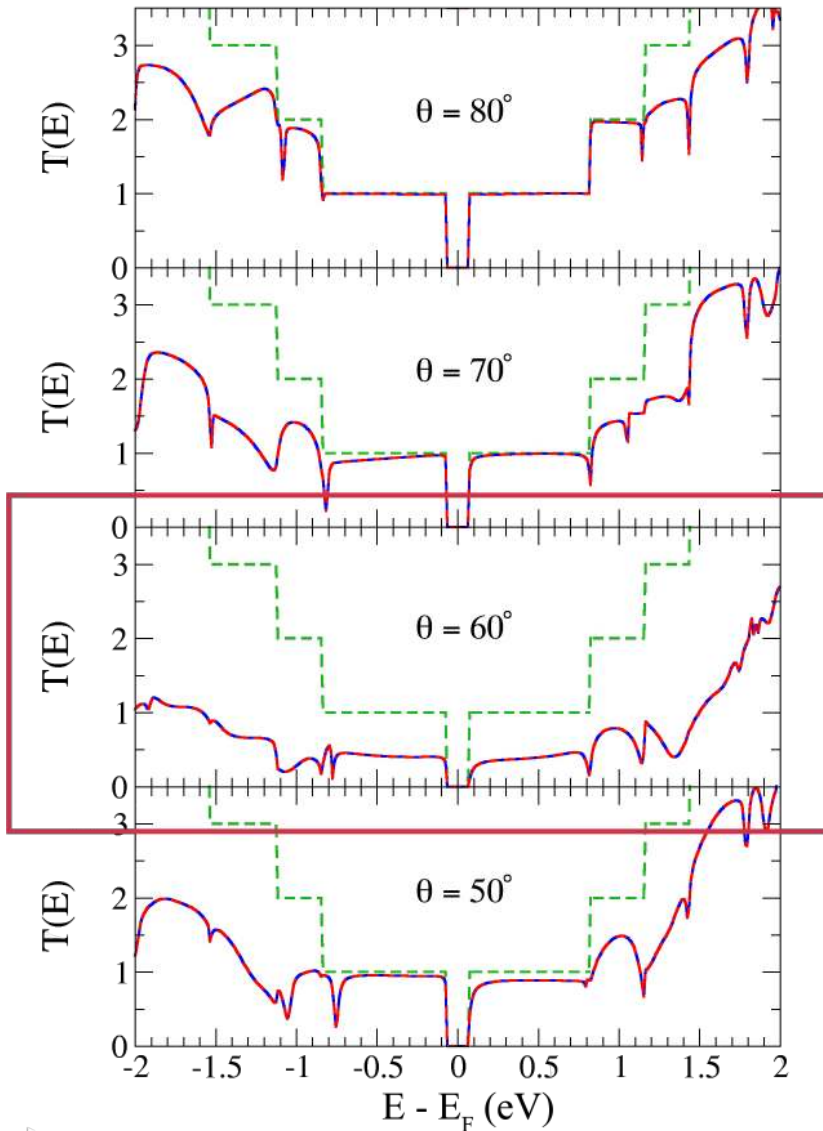
Electrostatic potential at $V = 0$



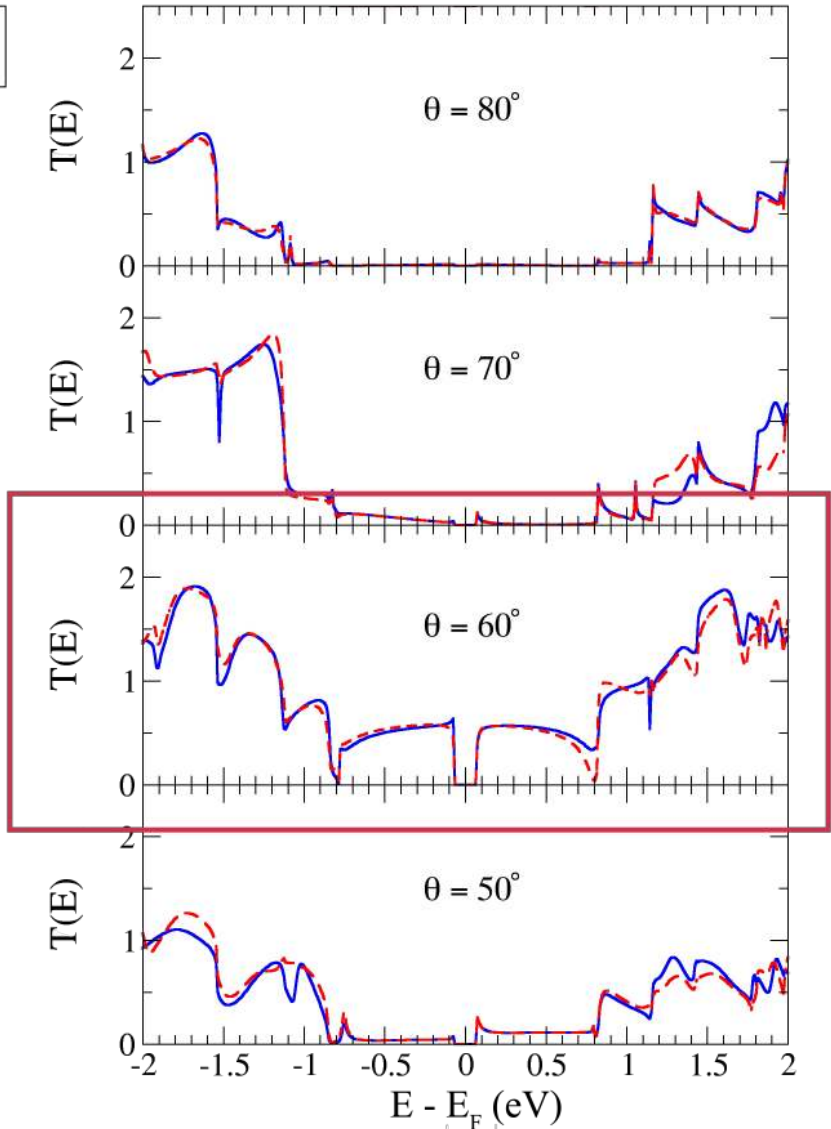
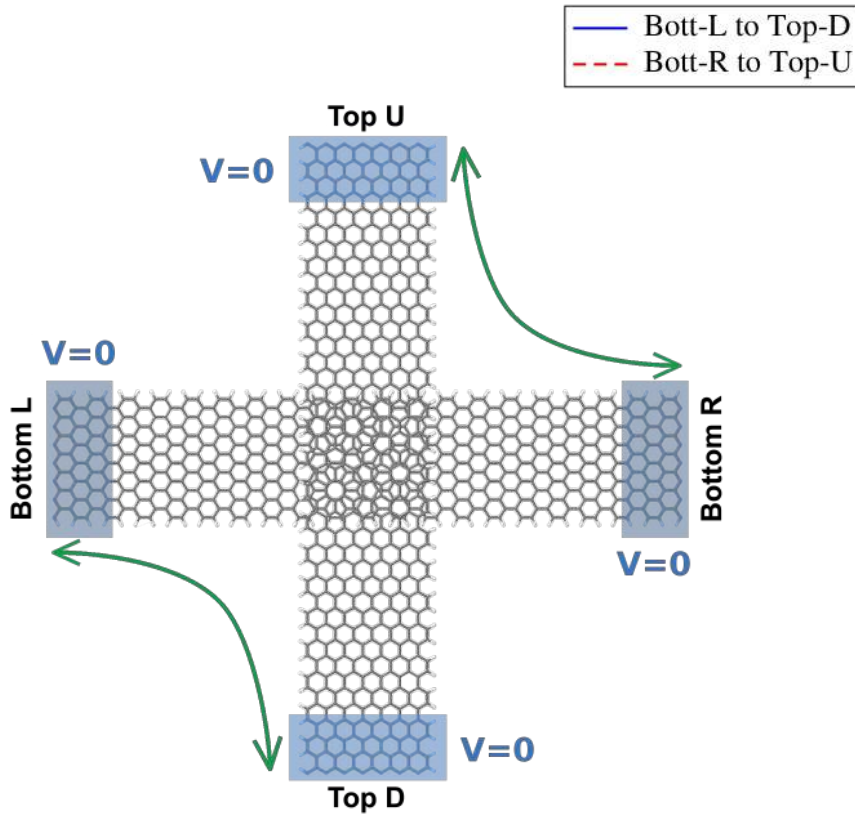
Direct transmission at $V = 0$



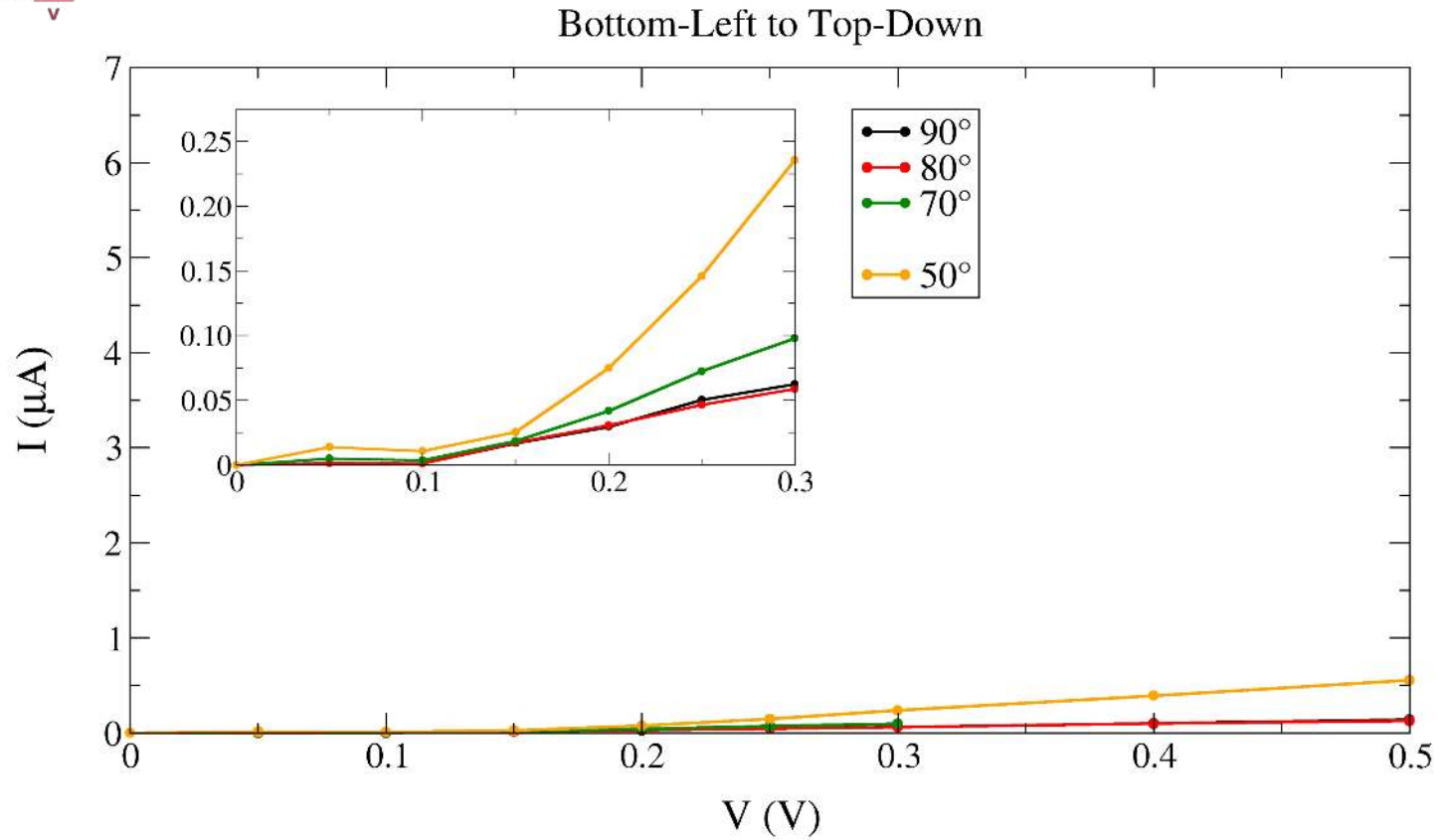
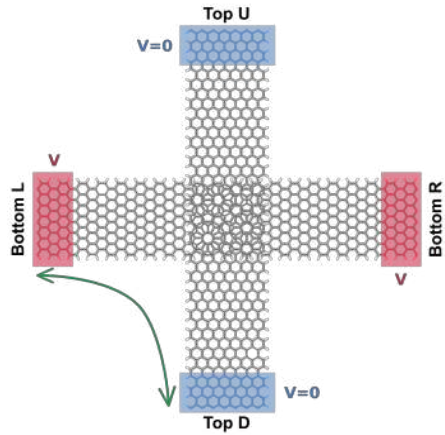
Direct transmission at $V = 0$



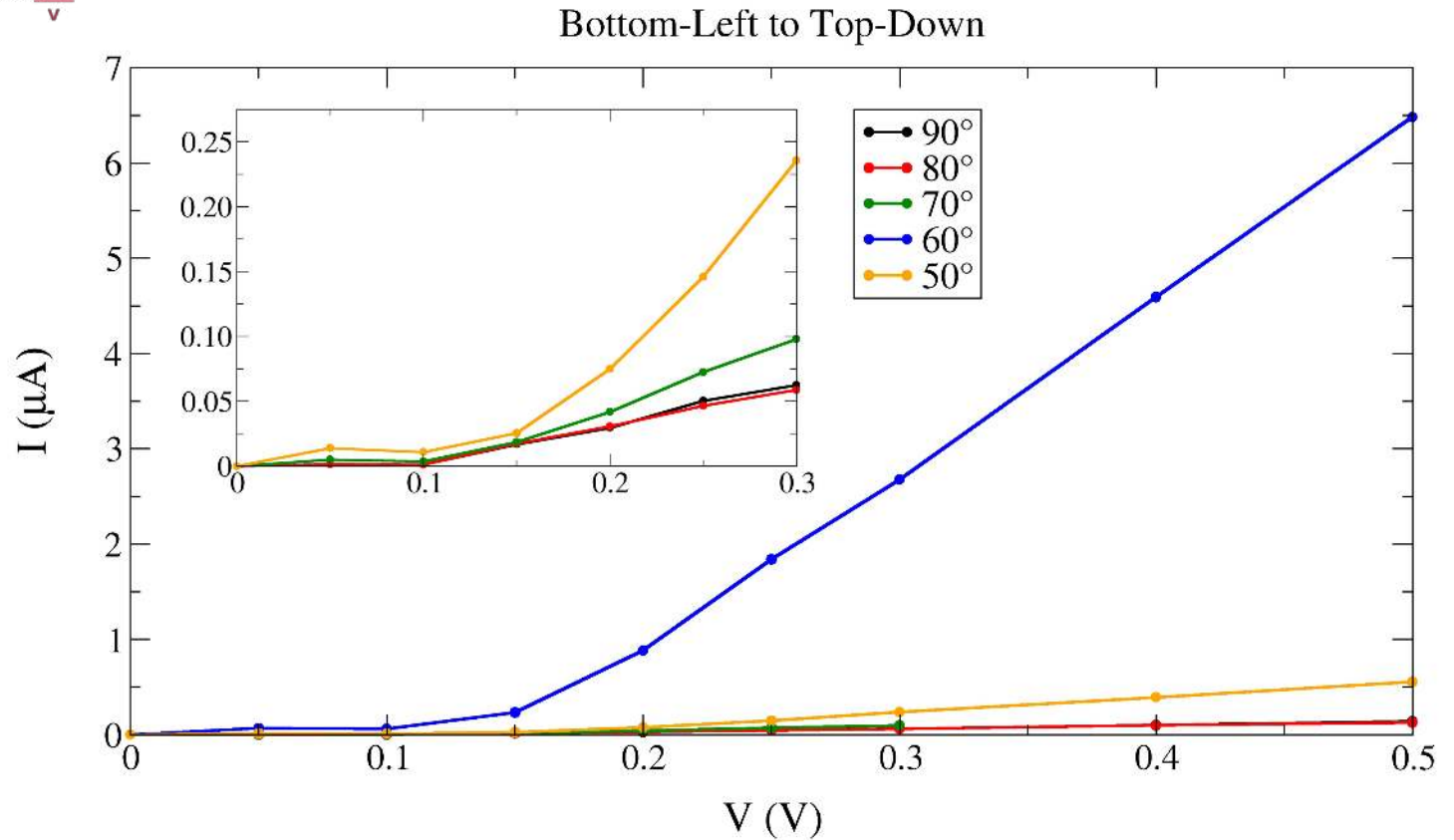
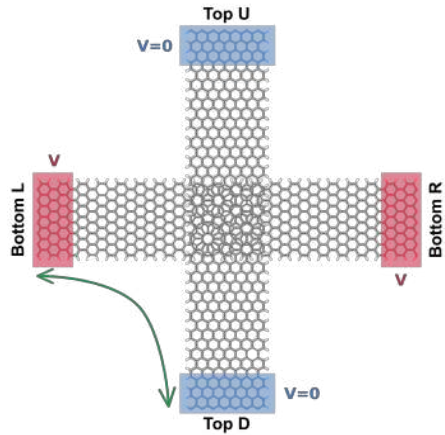
Inter-ribbon transmission at $V = 0$



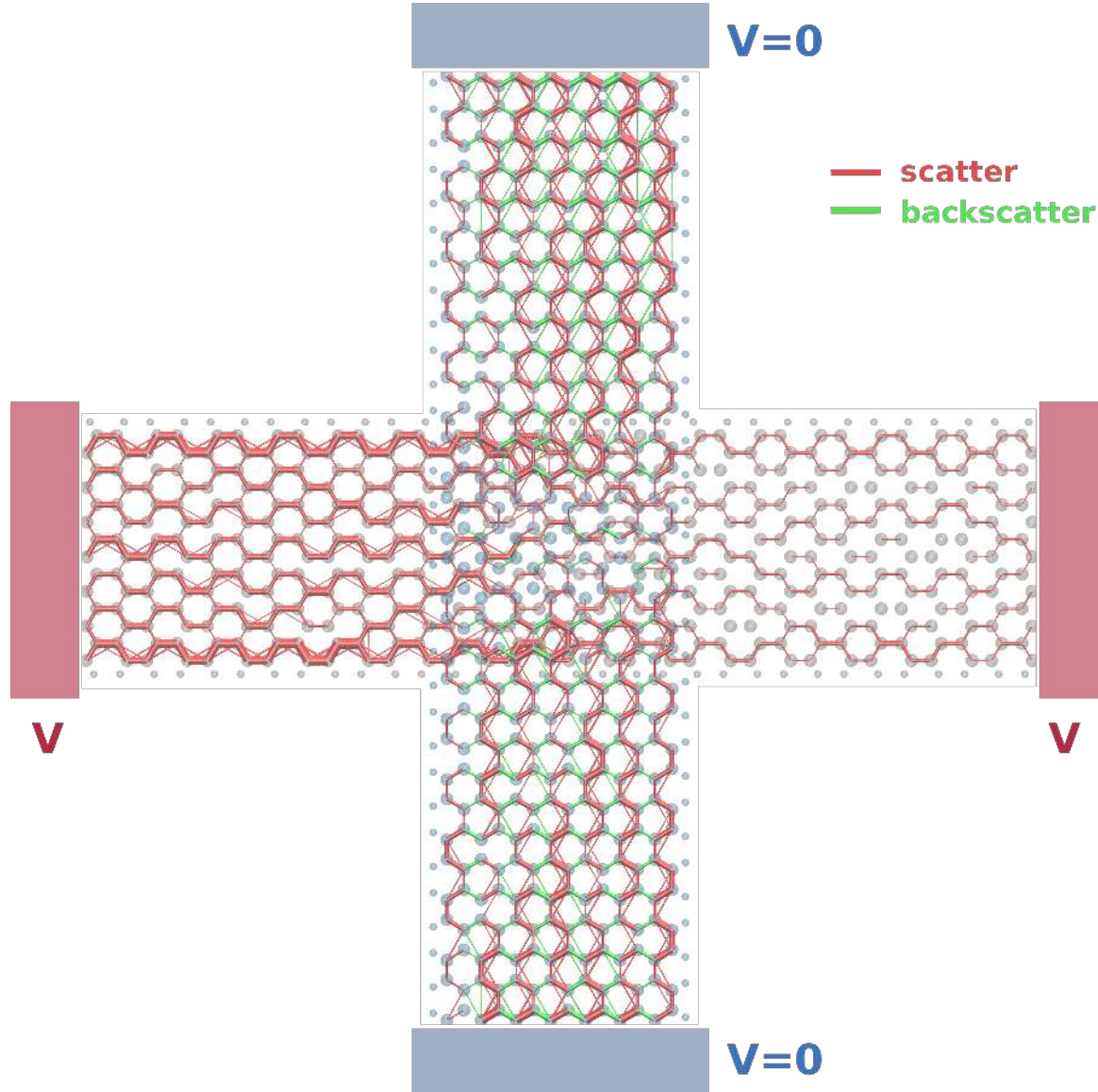
Inter-ribbon current



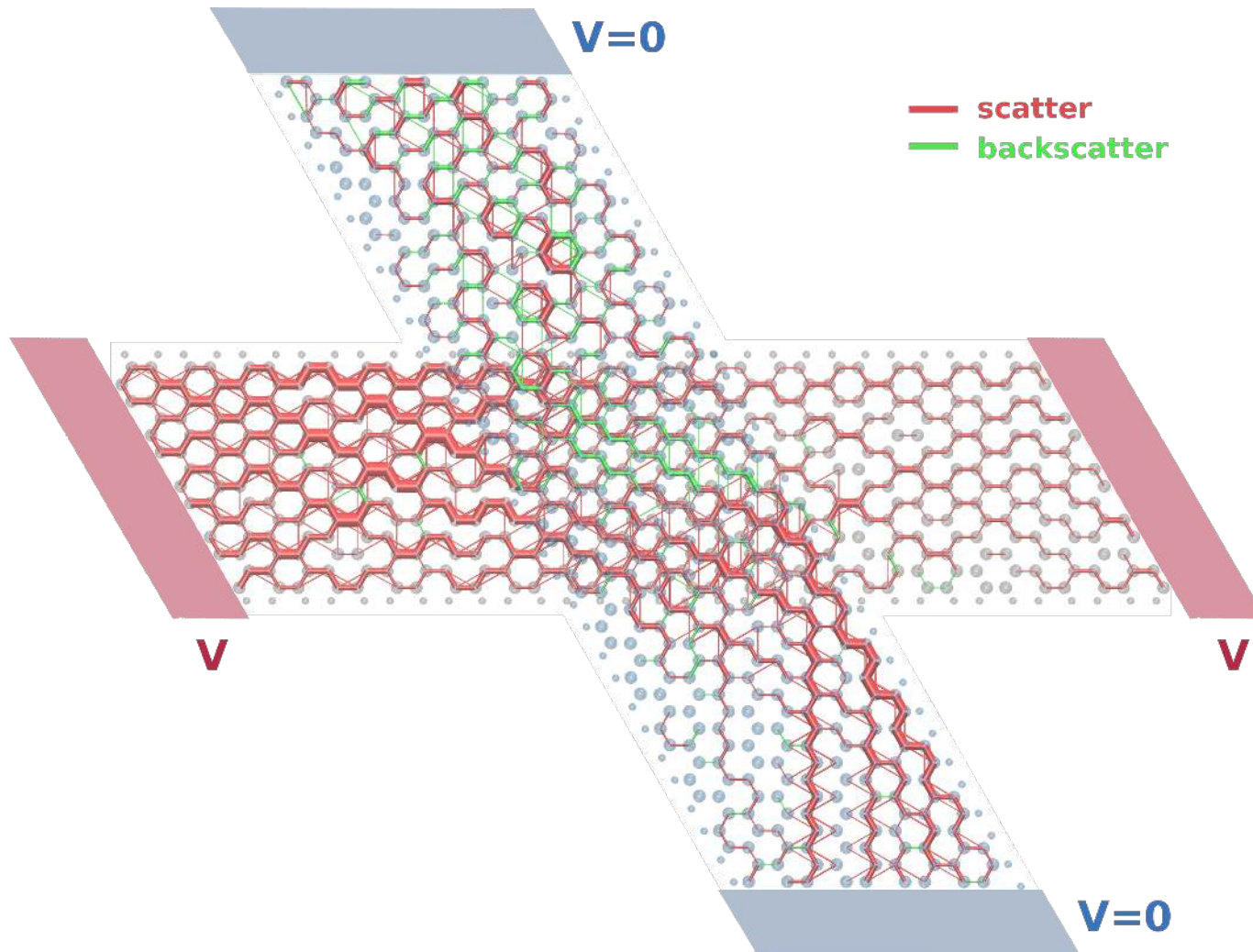
Inter-ribbon current



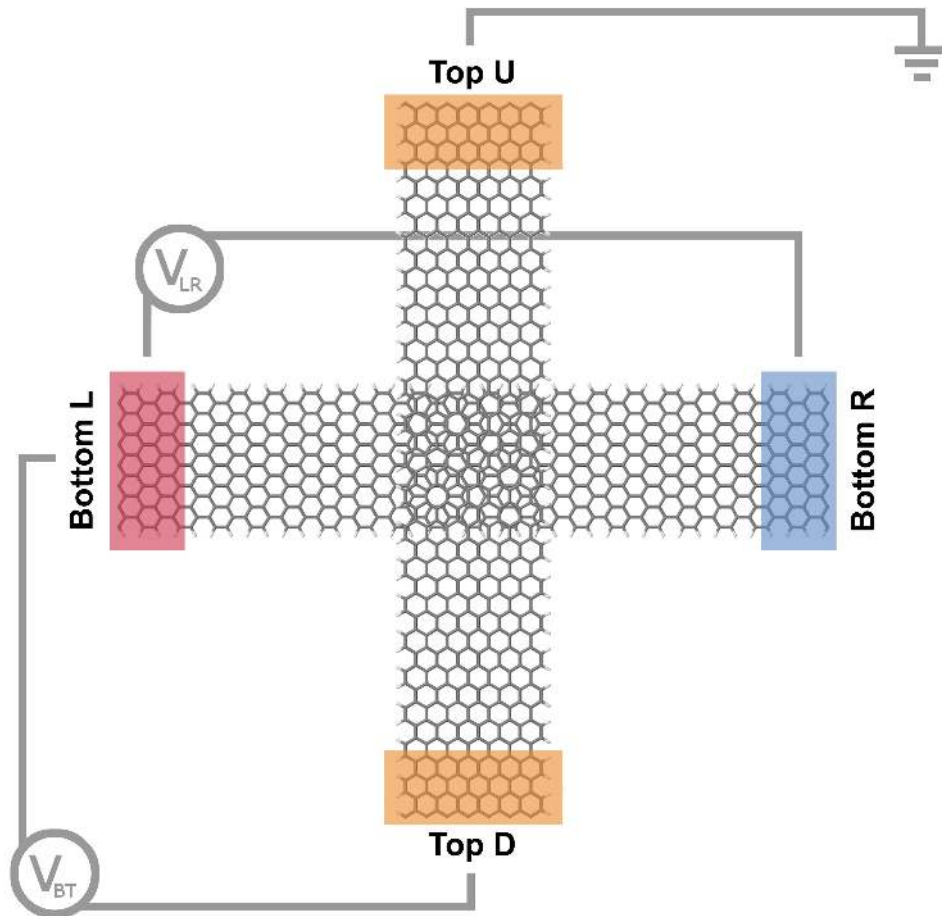
Bond currents for 90° at 0.5 V



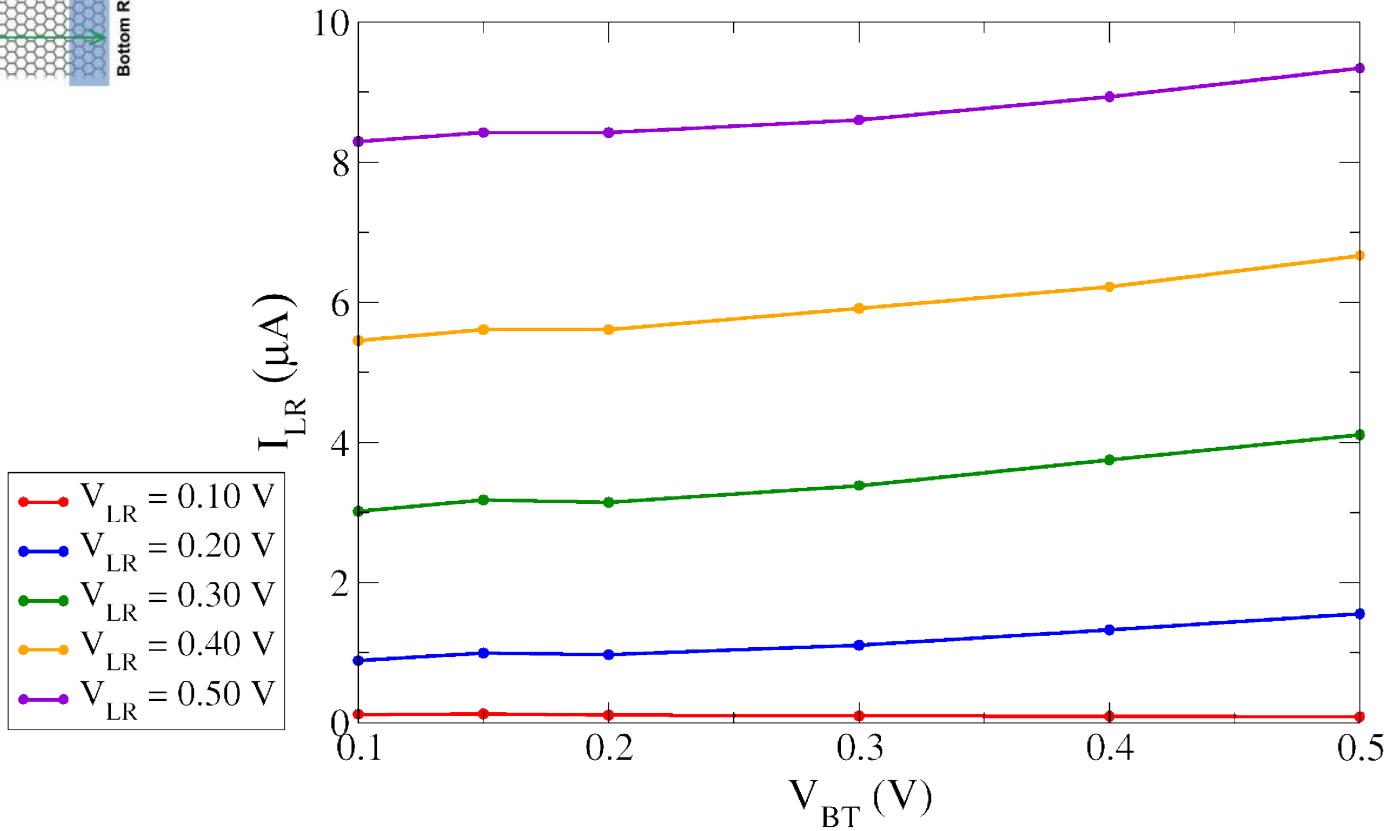
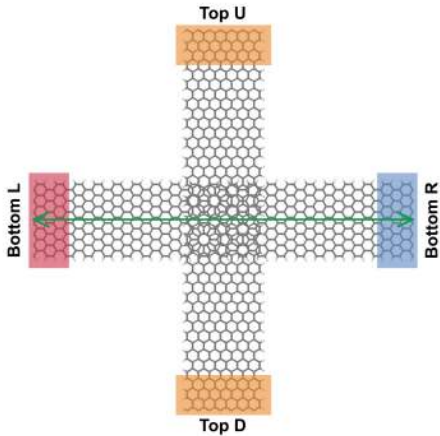
Bond currents for 60° at 0.5 V



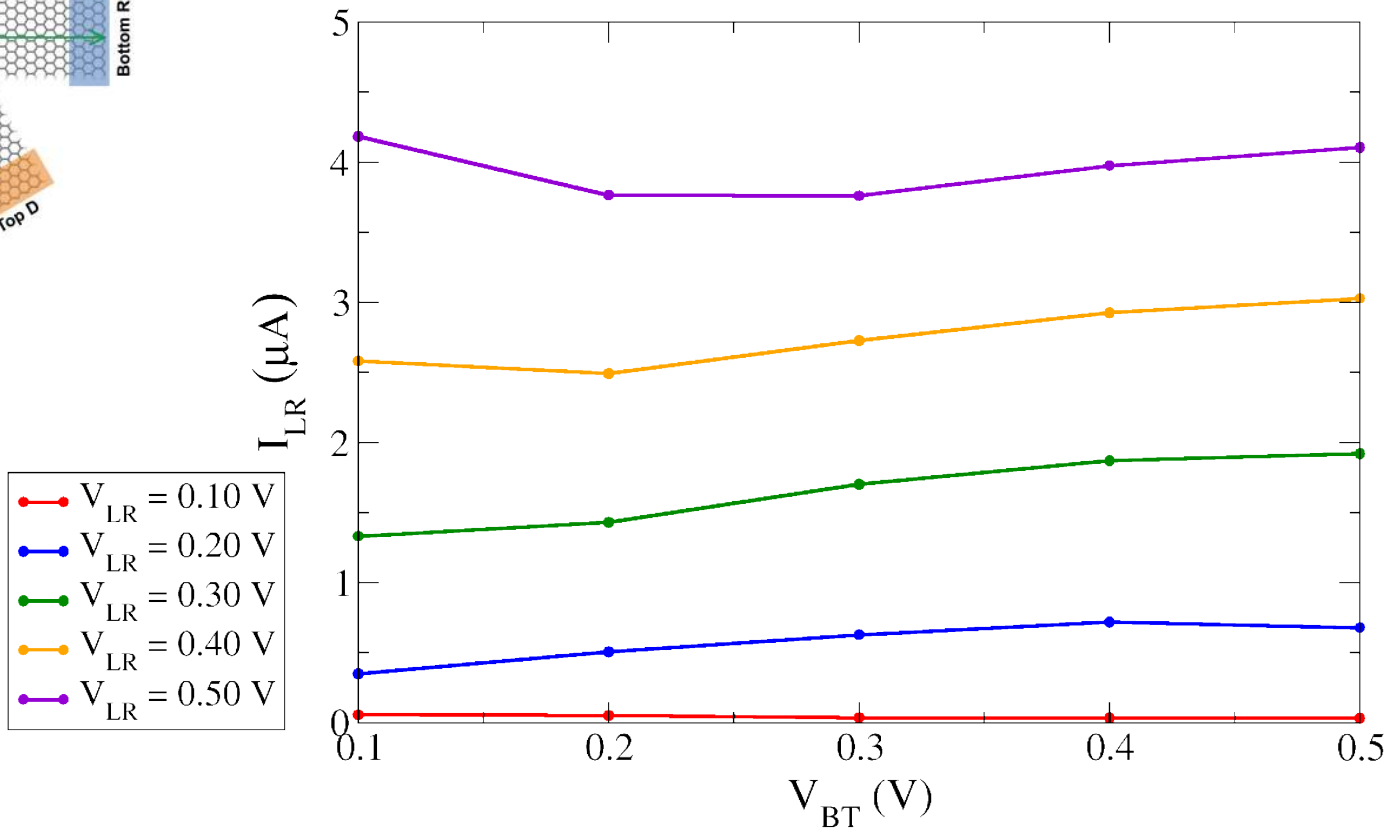
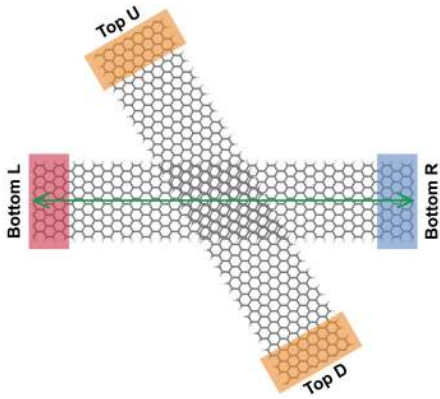
Intralayer bias



Intralayer bias



Intralayer bias




Conclusions

- Application of TranSIESTA for **N=4 arbitrarily distributed** electrodes at finite bias;
- Transmission **strongly depends on the stacking**;
- For a 60° rotation angle one finds a **higher inter-layer transmission**;
- In our calculations we observe a **small gating effect** due to the top ribbon.

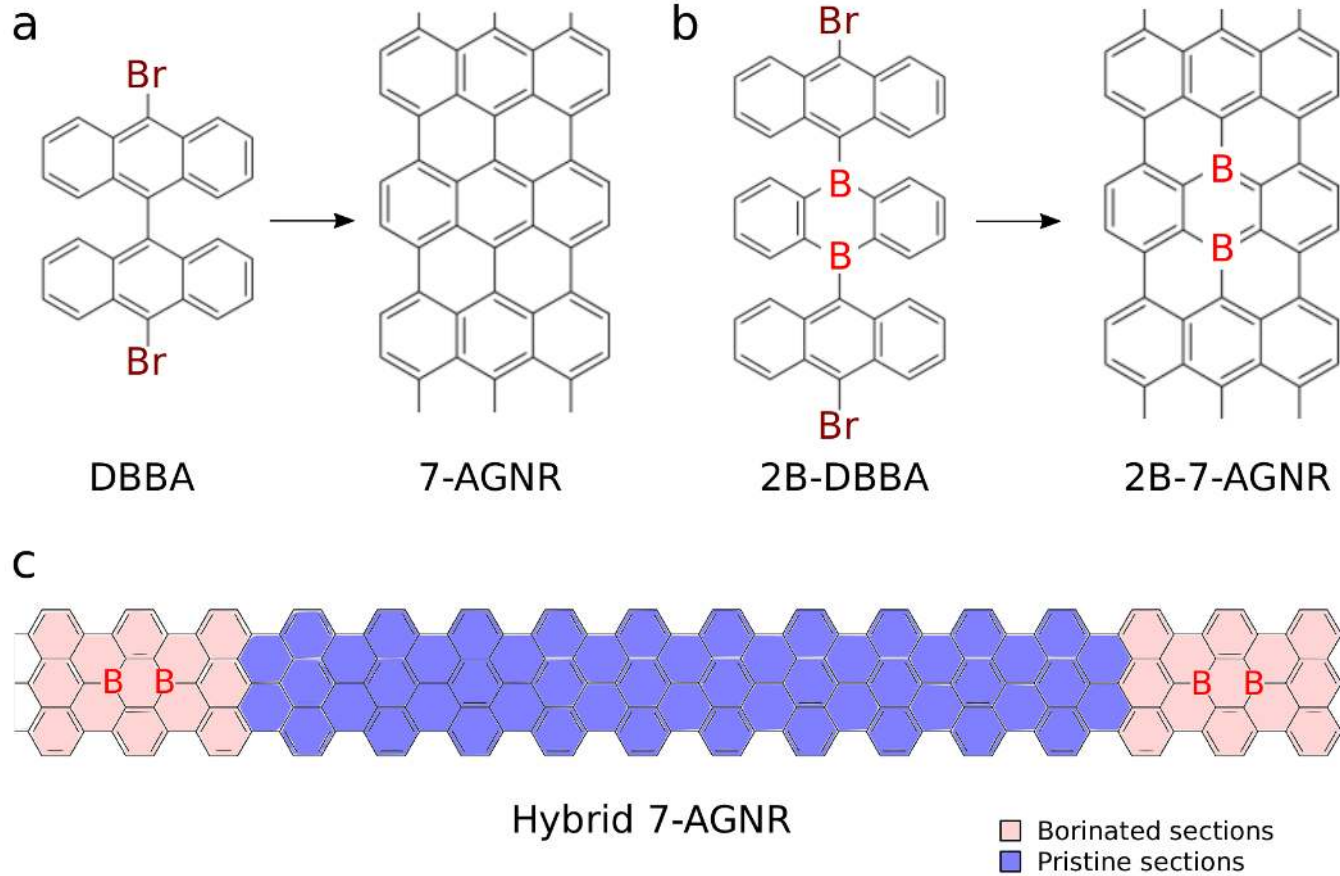


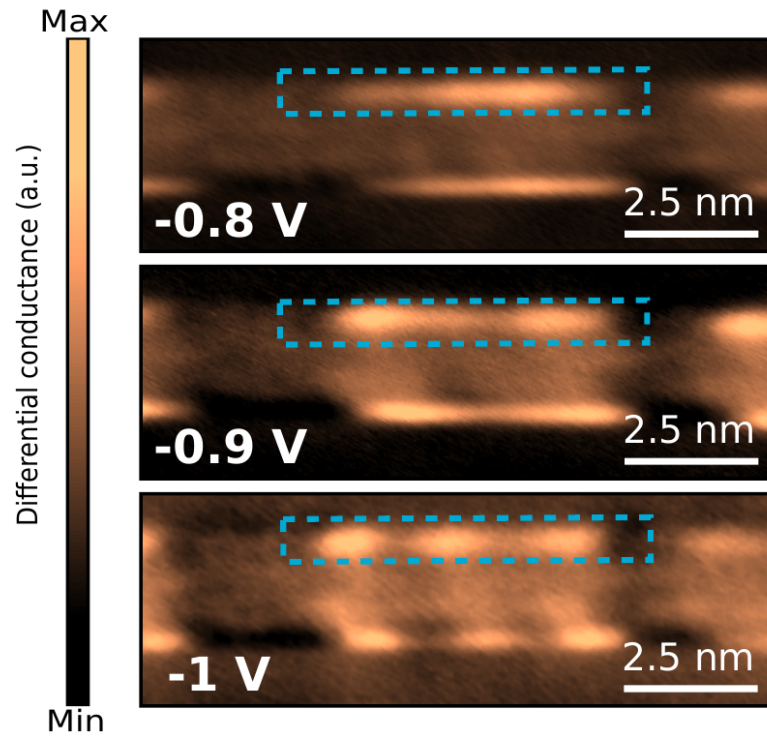
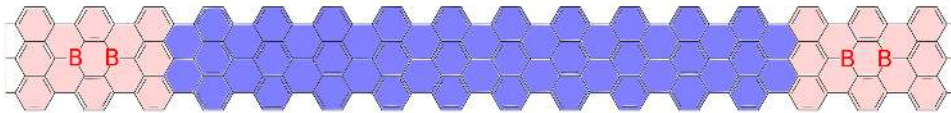
1-D Quantum Well States on Doped Graphene Nanoribbons Revealed by Transport Simulations

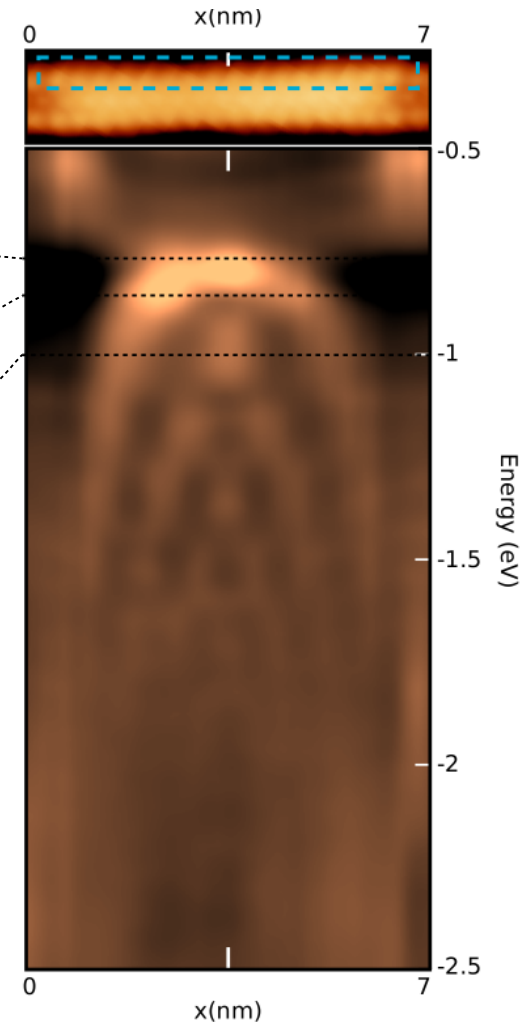
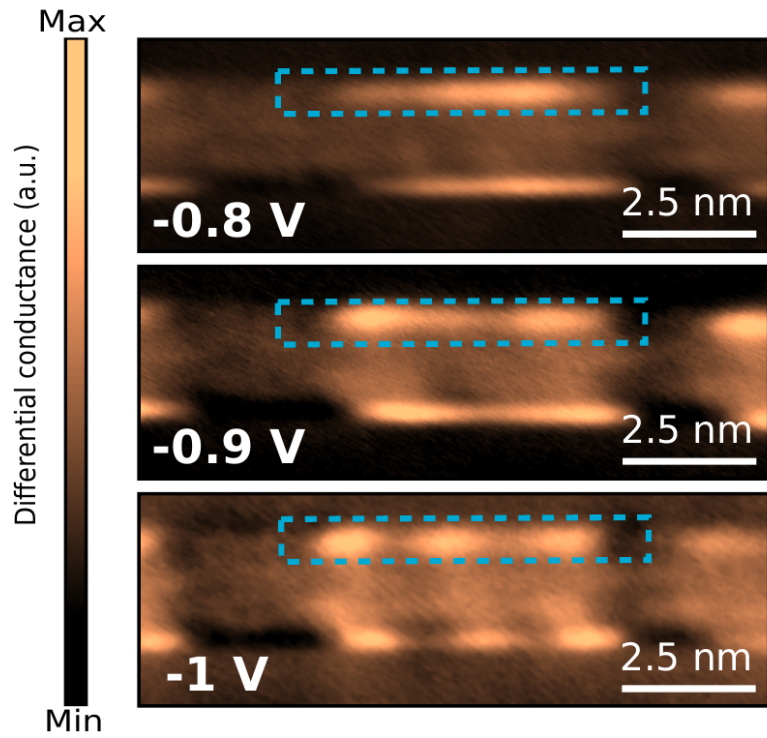
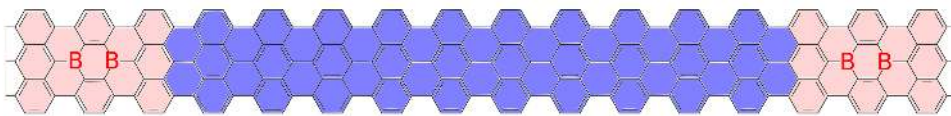


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Martina Corso, Richard Balog, Shigeki Kawaii, Shohei Saito, Shinichiro Osumi,
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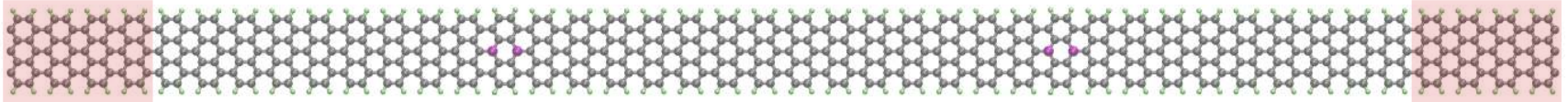
June 13, 2016



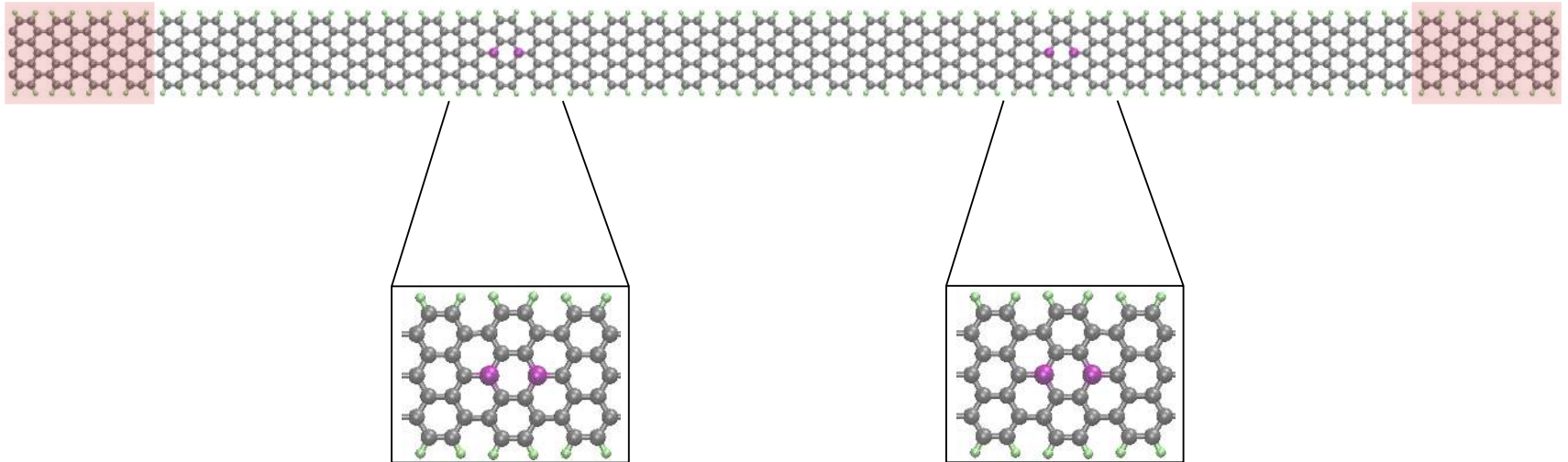




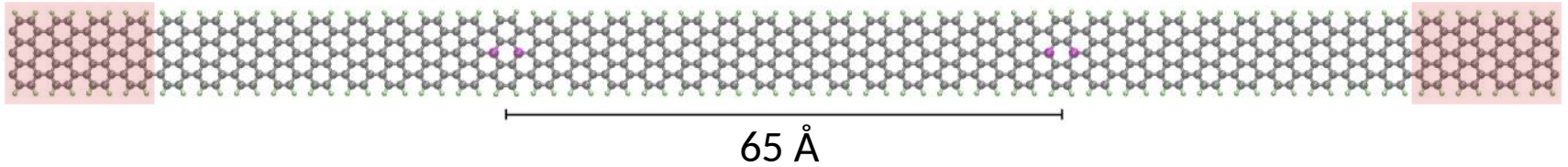
TranSIESTA



TranSIESTA



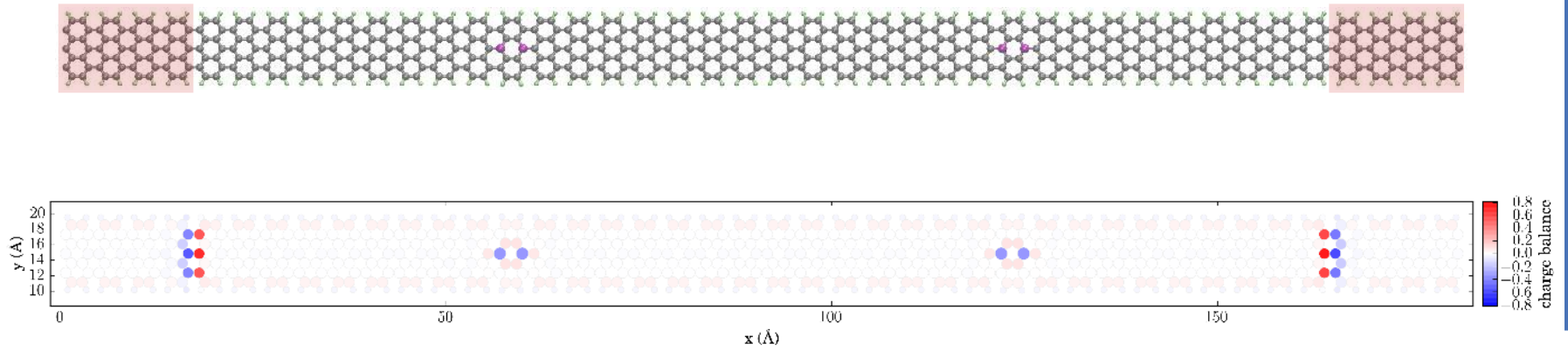
TranSIESTA



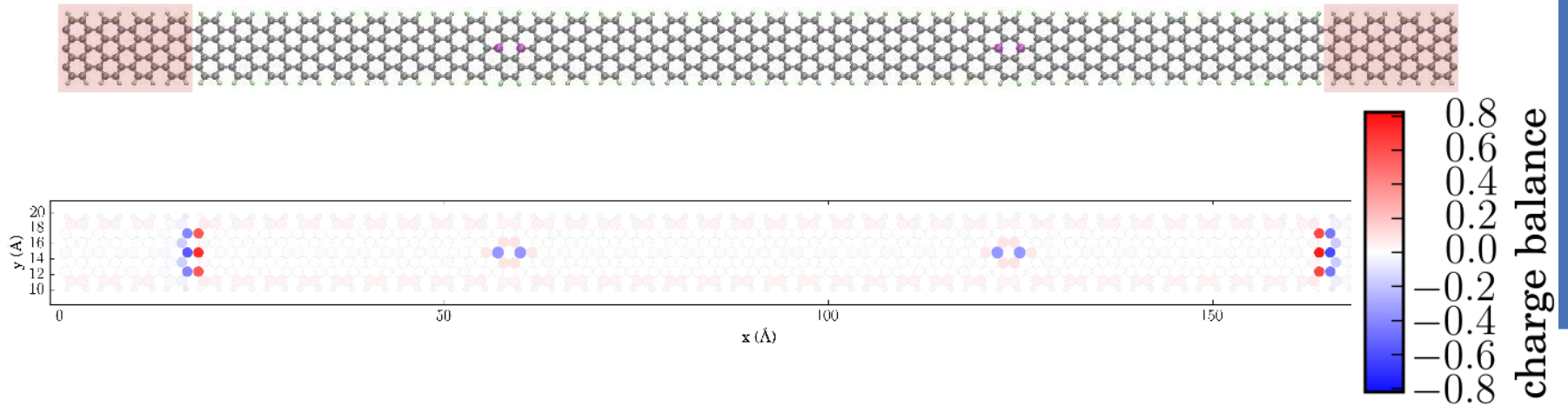
Simulation characteristics:

- 756 atoms;
- double- ζ (5040 orbitals);
- vdW (optB88);
- real space grid cutoff: 250 Ry;
- forces < 10 meV/Å.

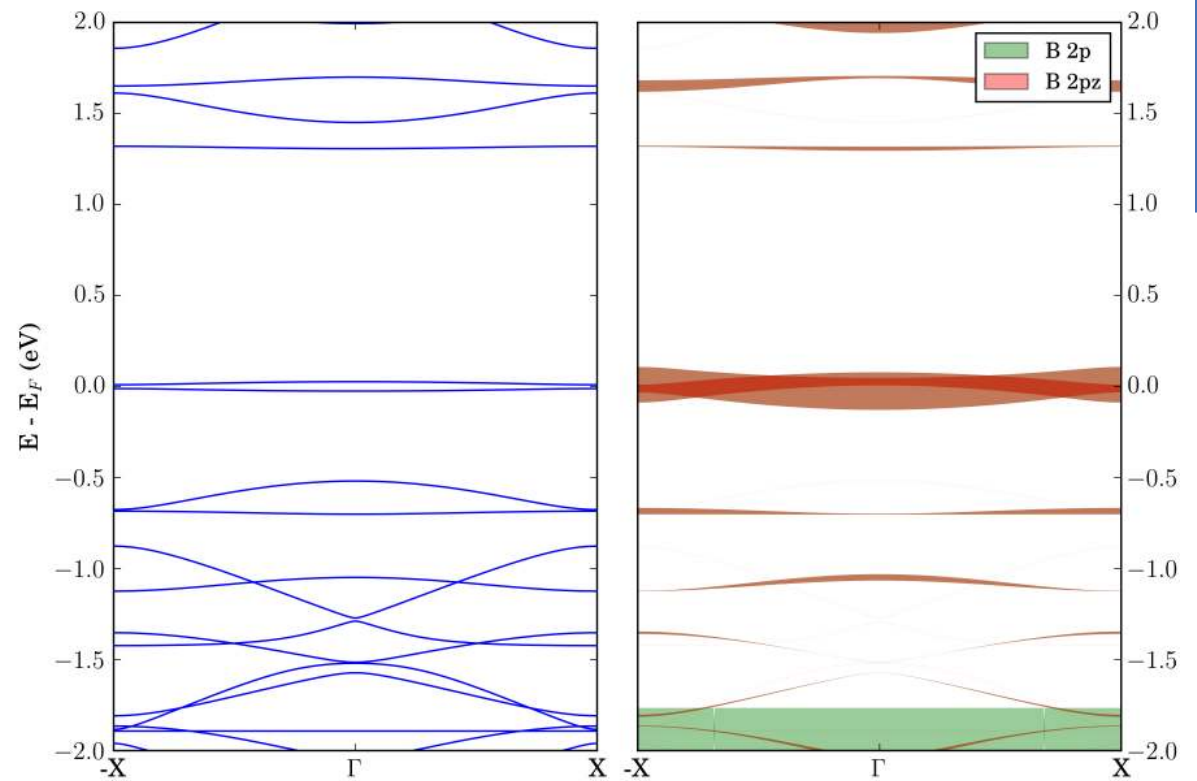
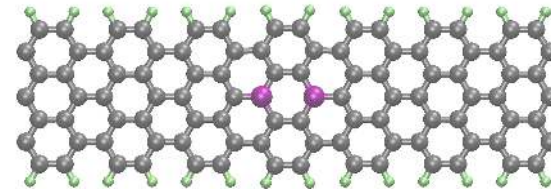
Mulliken population



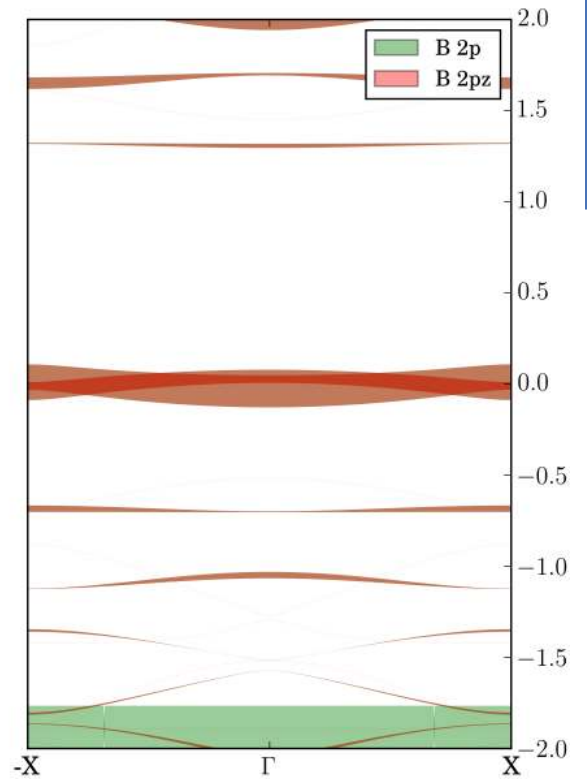
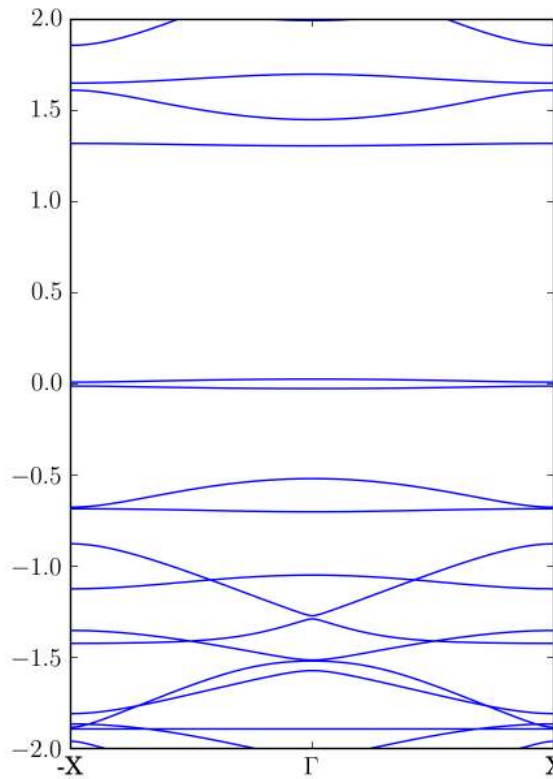
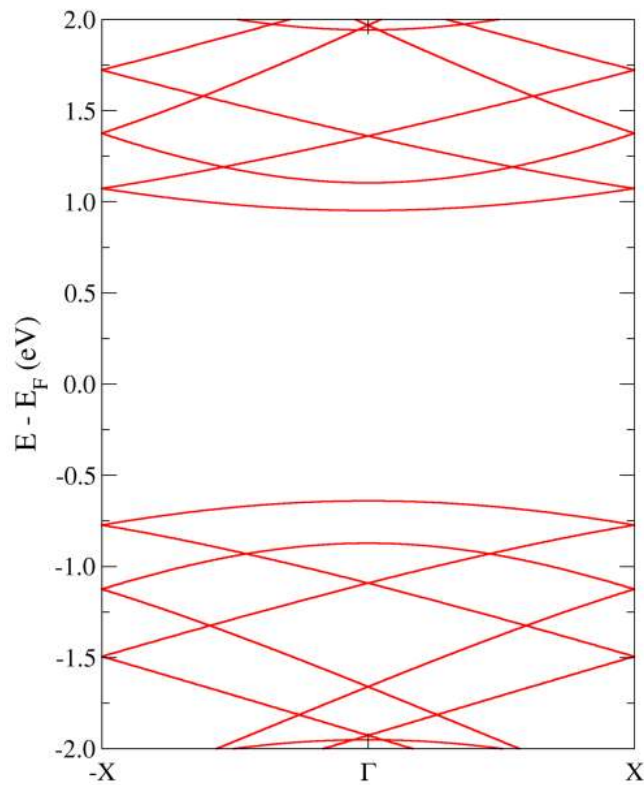
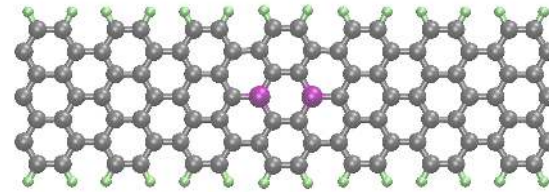
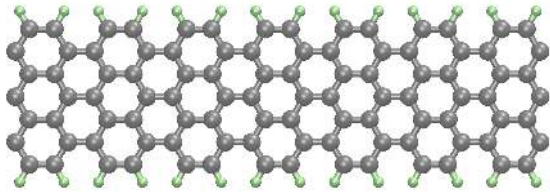
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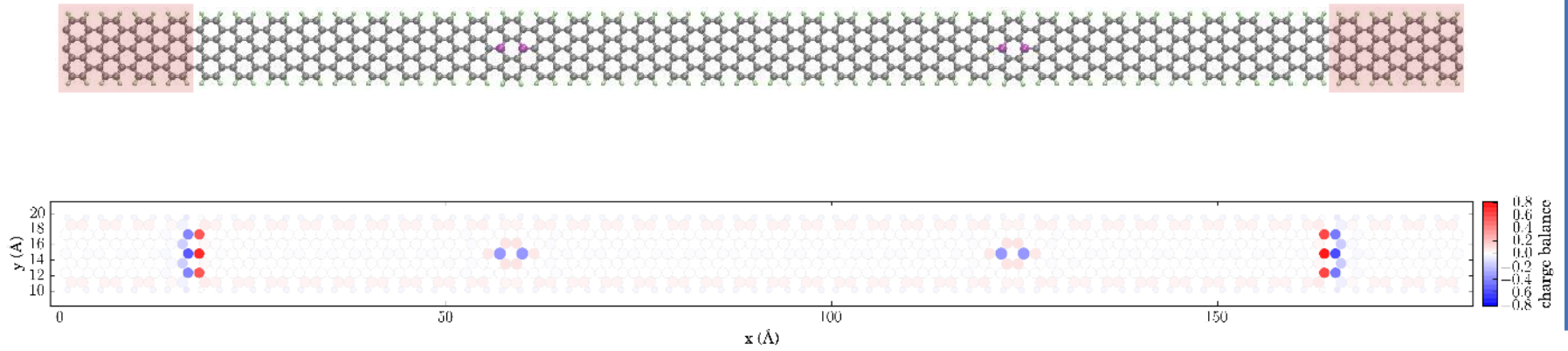
Periodic calculation



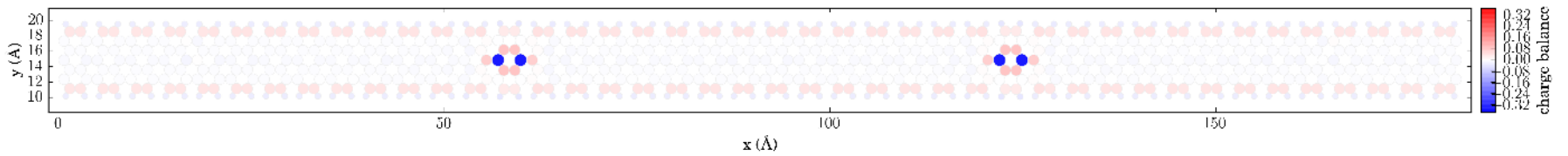
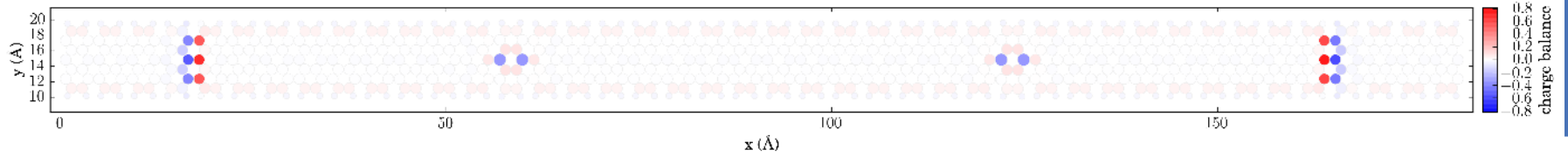
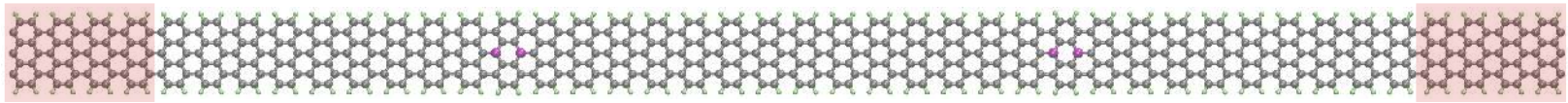
Periodic calculation



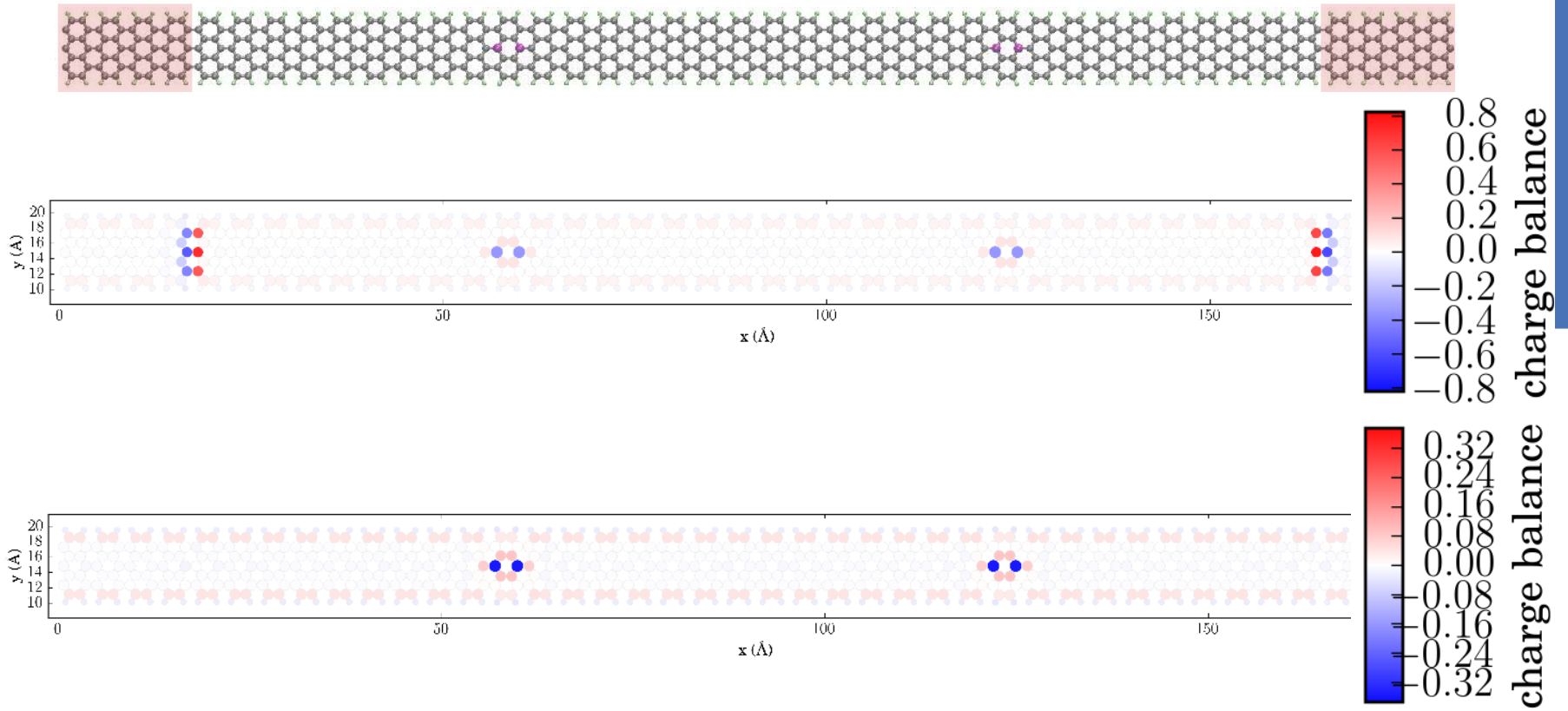
Mulliken population



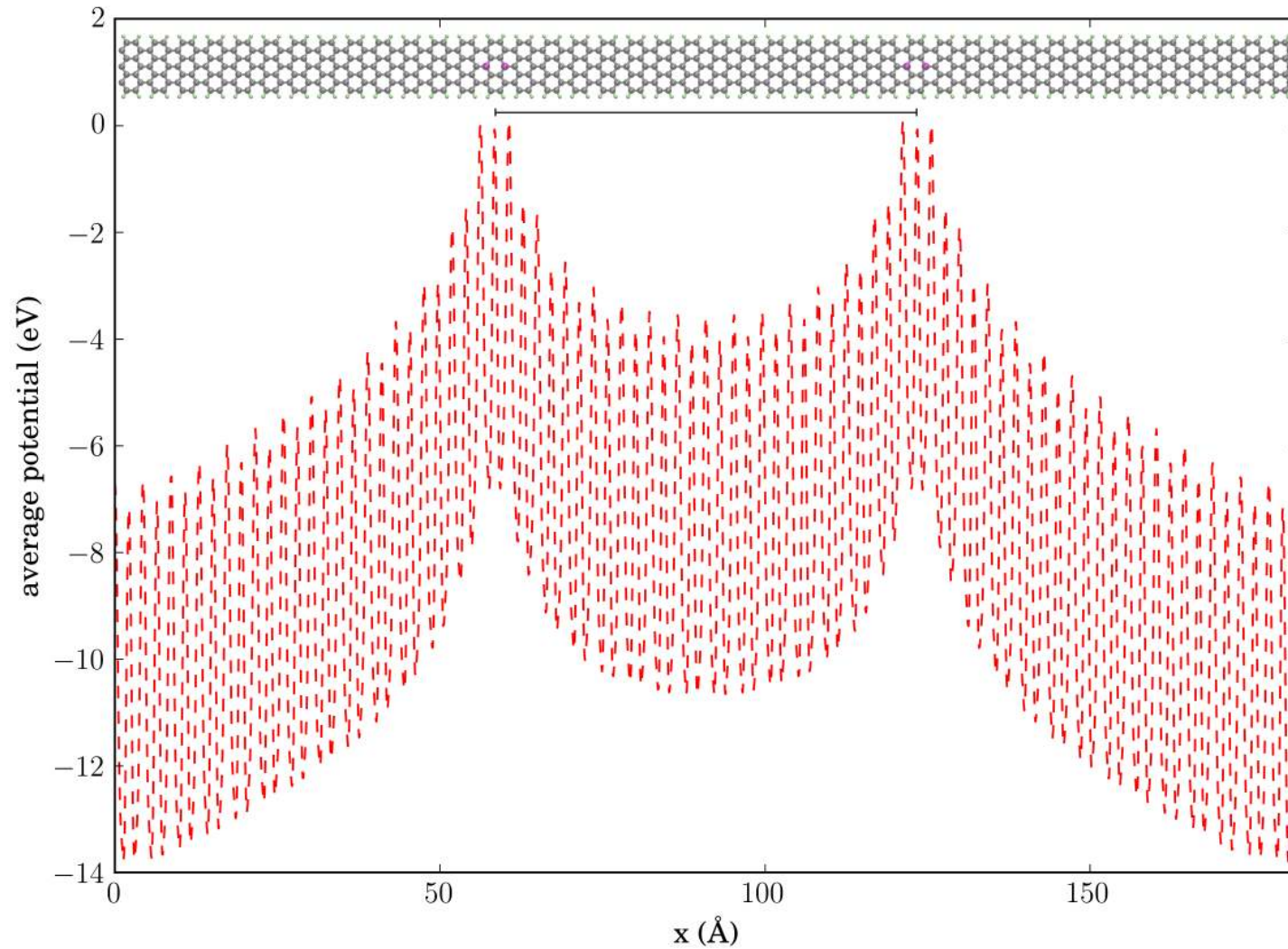
Mulliken population



Mulliken population



Electrostatic potential



Coulomb cutoff

$$\tilde{v}(\mathbf{G}) = \int \int \int_{space} \tilde{v}(r) e^{-i\mathbf{G}\cdot\mathbf{r}} d^3\mathbf{r} = \int \int \int_{\mathcal{D}} v(r) e^{-i\mathbf{G}\cdot\mathbf{r}} d^3\mathbf{r}$$

Coulomb cutoff

$$\tilde{v}(\mathbf{G}) = \int \int \int_{space} \tilde{v}(r) e^{-i\mathbf{G}\cdot\mathbf{r}} d^3\mathbf{r} = \int \int \int_{\mathcal{D}} v(r) e^{-i\mathbf{G}\cdot\mathbf{r}} d^3\mathbf{r}$$

- 0-D: $\tilde{v}^{0D}(G) = \frac{4\pi}{G^2} [1 - \cos(GR)]$

Coulomb cutoff

$$\tilde{v}(\mathbf{G}) = \int \int \int_{space} \tilde{v}(r) e^{-i\mathbf{G}\cdot\mathbf{r}} d^3\mathbf{r} = \int \int \int_{\mathcal{D}} v(r) e^{-i\mathbf{G}\cdot\mathbf{r}} d^3\mathbf{r}$$

- 0-D: $\tilde{v}^{0D}(G) = \frac{4\pi}{G^2} [1 - \cos(GR)]$
- 1-D: $\tilde{v}^{1D}(G_x, G_\perp) = \frac{4\pi}{G^2} [1 + G_\perp R J_1(G_\perp R) K_0(G_x R) - G_x R J_0(G_\perp R) K_1(G_x R)]$

Coulomb cutoff

$$\tilde{v}(\mathbf{G}) = \int \int \int_{space} \tilde{v}(r) e^{-i\mathbf{G}\cdot\mathbf{r}} d^3\mathbf{r} = \int \int \int_{\mathcal{D}} v(r) e^{-i\mathbf{G}\cdot\mathbf{r}} d^3\mathbf{r}$$

- 0-D: $\tilde{v}^{0D}(G) = \frac{4\pi}{G^2} [1 - \cos(GR)]$

- 1-D: $\tilde{v}^{1D}(G_x, G_\perp) = \frac{4\pi}{G^2} [1 + G_\perp R J_1(G_\perp R) K_0(G_x R) - G_x R J_0(G_\perp R) K_1(G_x R)]$

$$\approx -4\pi \int_0^R r J_0(G_\perp r) \ln(r) dr + 4\pi R \ln(2h) \frac{J_1(G_\perp R)}{G_\perp}$$

Coulomb cutoff

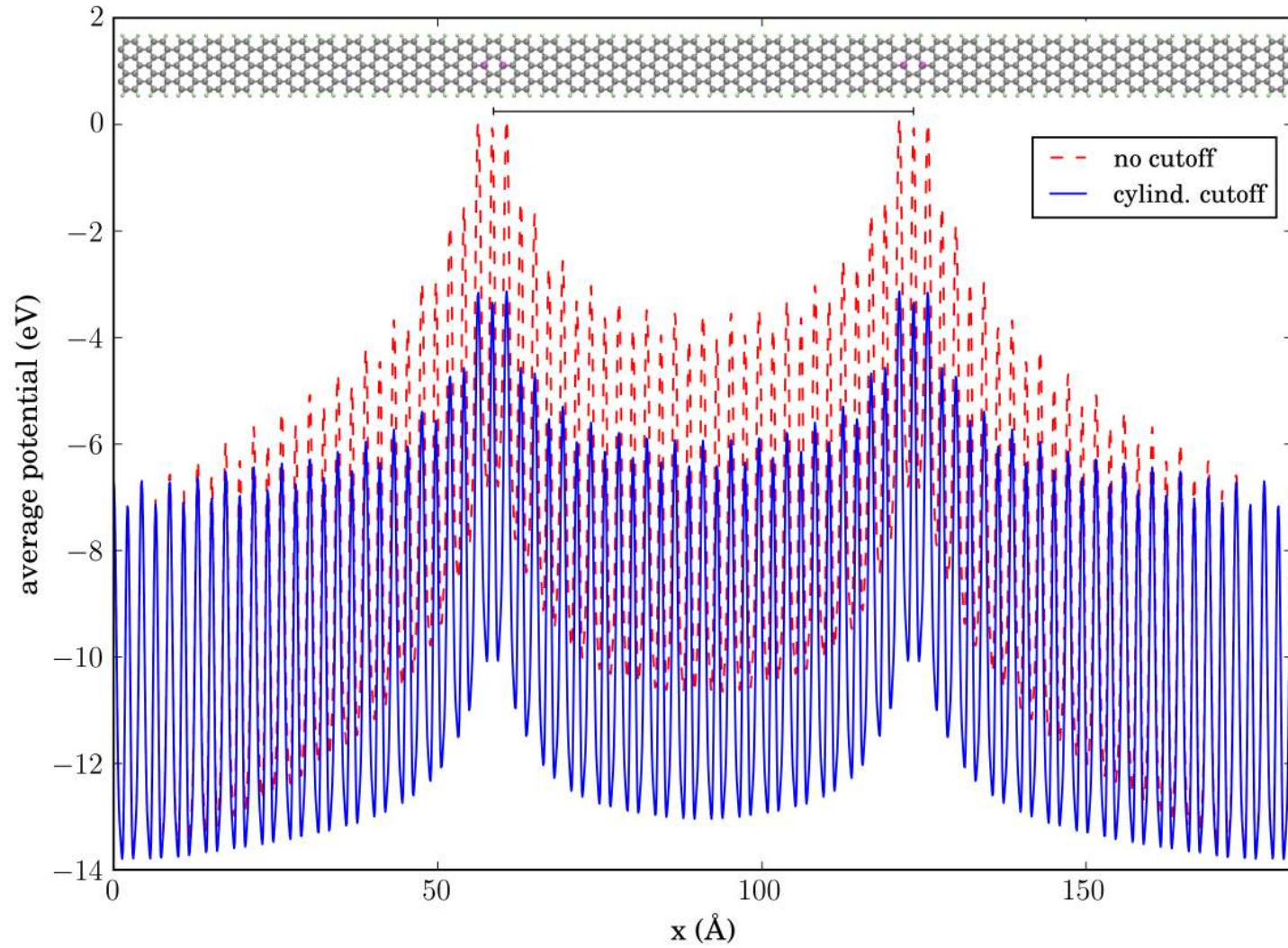
$$\tilde{v}(\mathbf{G}) = \int \int \int_{space} \tilde{v}(r) e^{-i\mathbf{G}\cdot\mathbf{r}} d^3\mathbf{r} = \int \int \int_{\mathcal{D}} v(r) e^{-i\mathbf{G}\cdot\mathbf{r}} d^3\mathbf{r}$$

- 0-D: $\tilde{v}^{0D}(G) = \frac{4\pi}{G^2} [1 - \cos(GR)]$

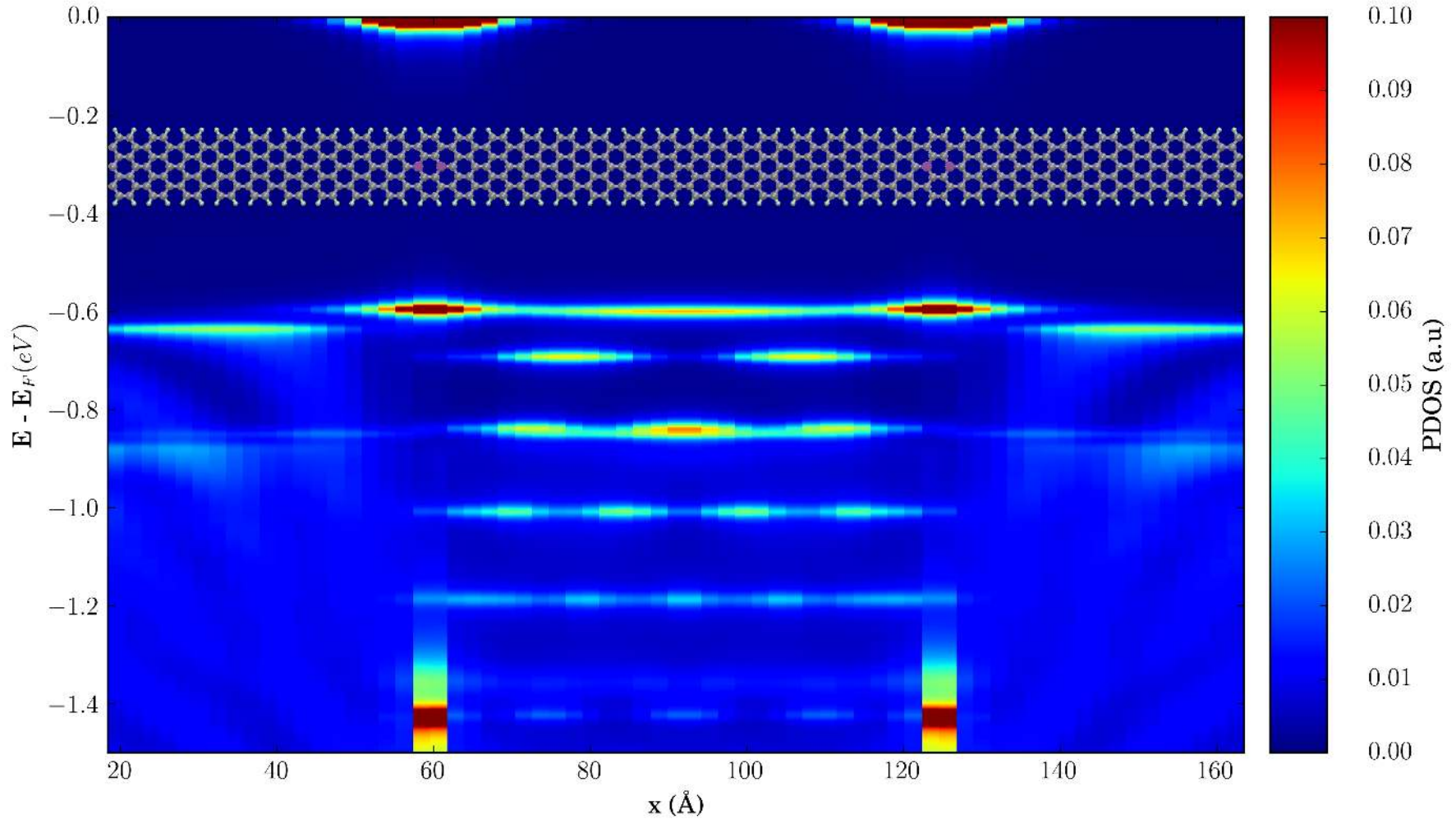
- 1-D: $\tilde{v}^{1D}(G_x, G_\perp) = \frac{4\pi}{G^2} [1 + G_\perp R J_1(G_\perp R) K_0(G_x R) - G_x R J_0(G_\perp R) K_1(G_x R)]$

$$\approx -4\pi \int_0^R r J_0(G_\perp r) \ln(r) dr + 4\pi R \ln(2\hbar) \frac{J_1(G_\perp R)}{G_\perp} = 0$$

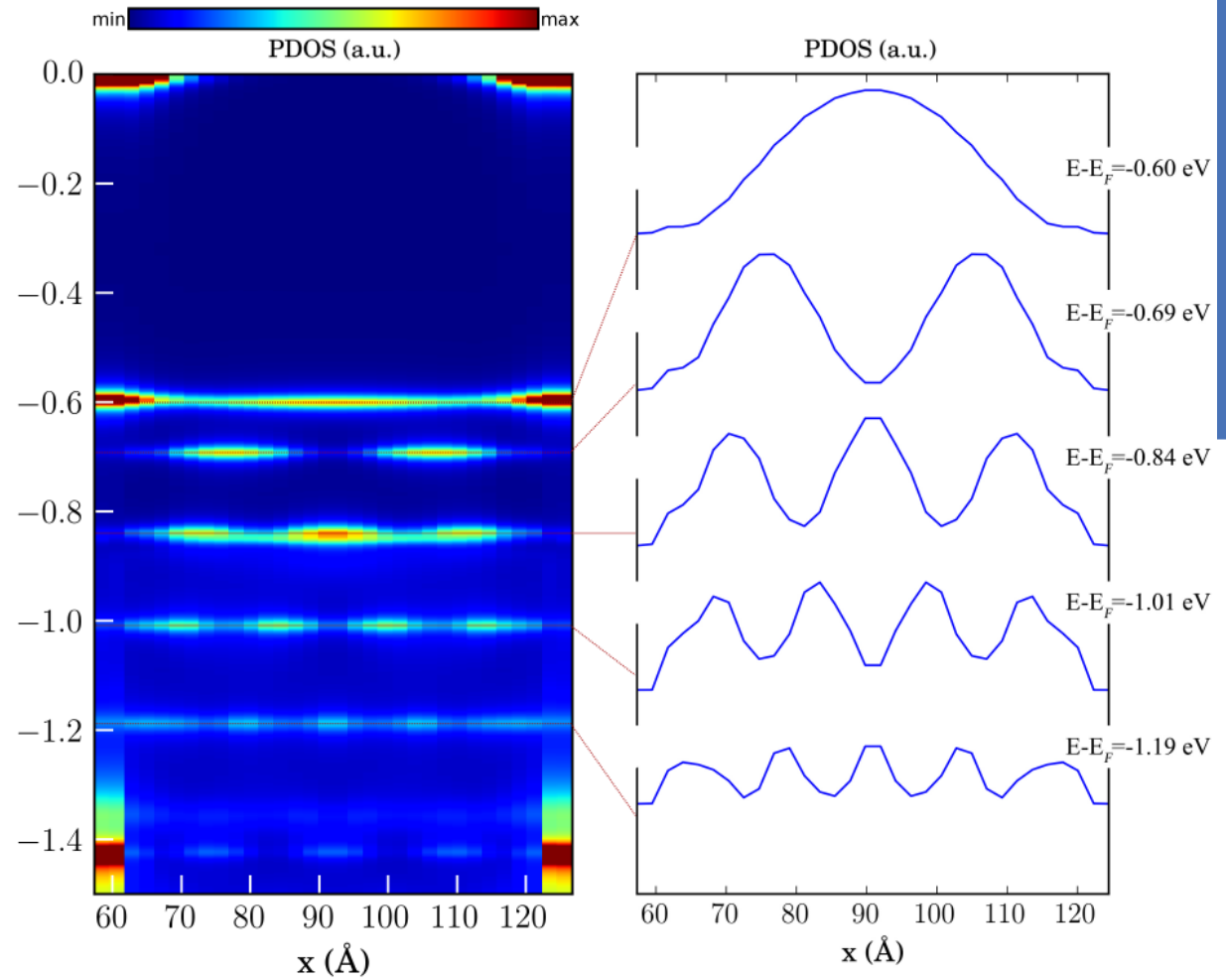
Electrostatic potential



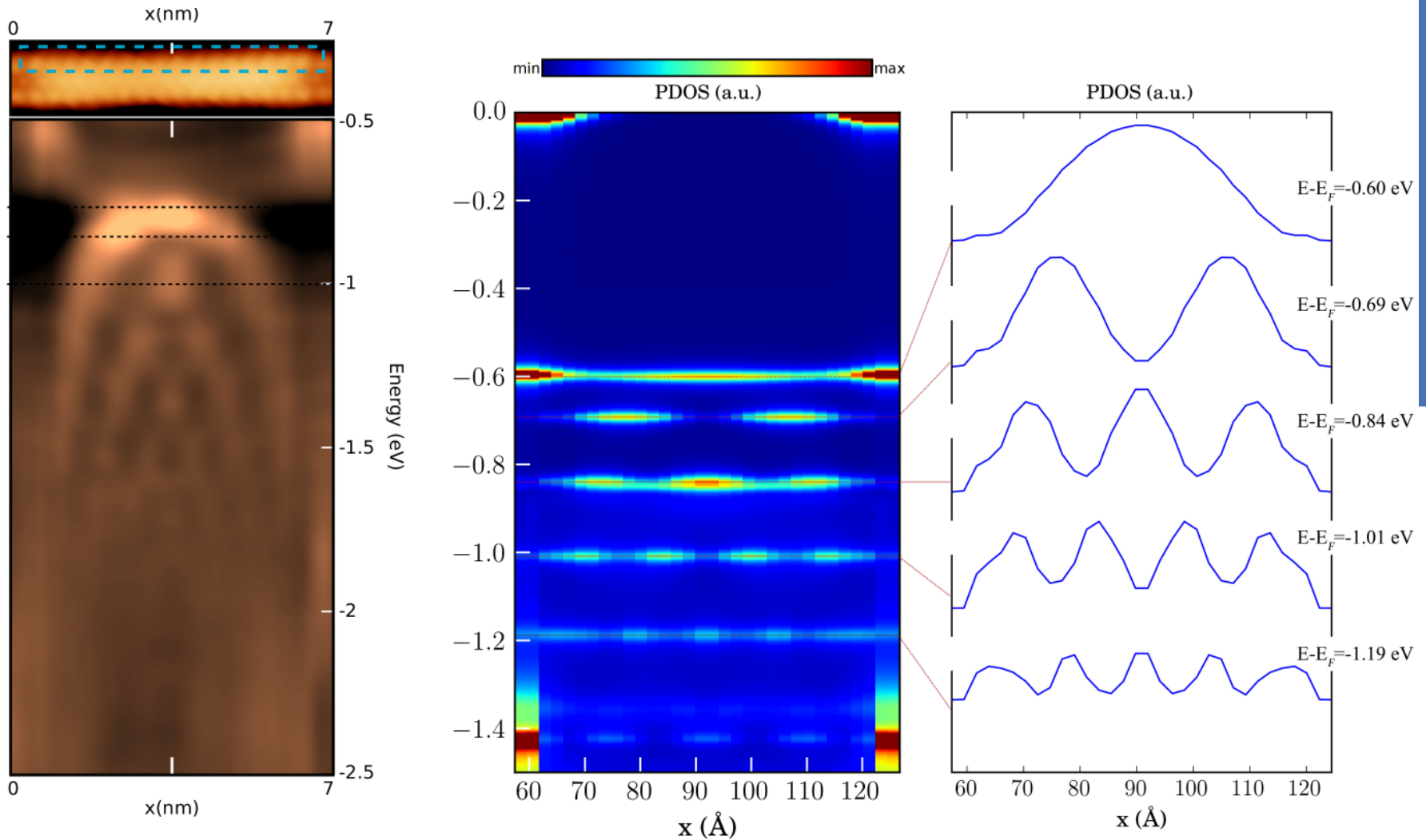
DOS projected on each ribbon "row"



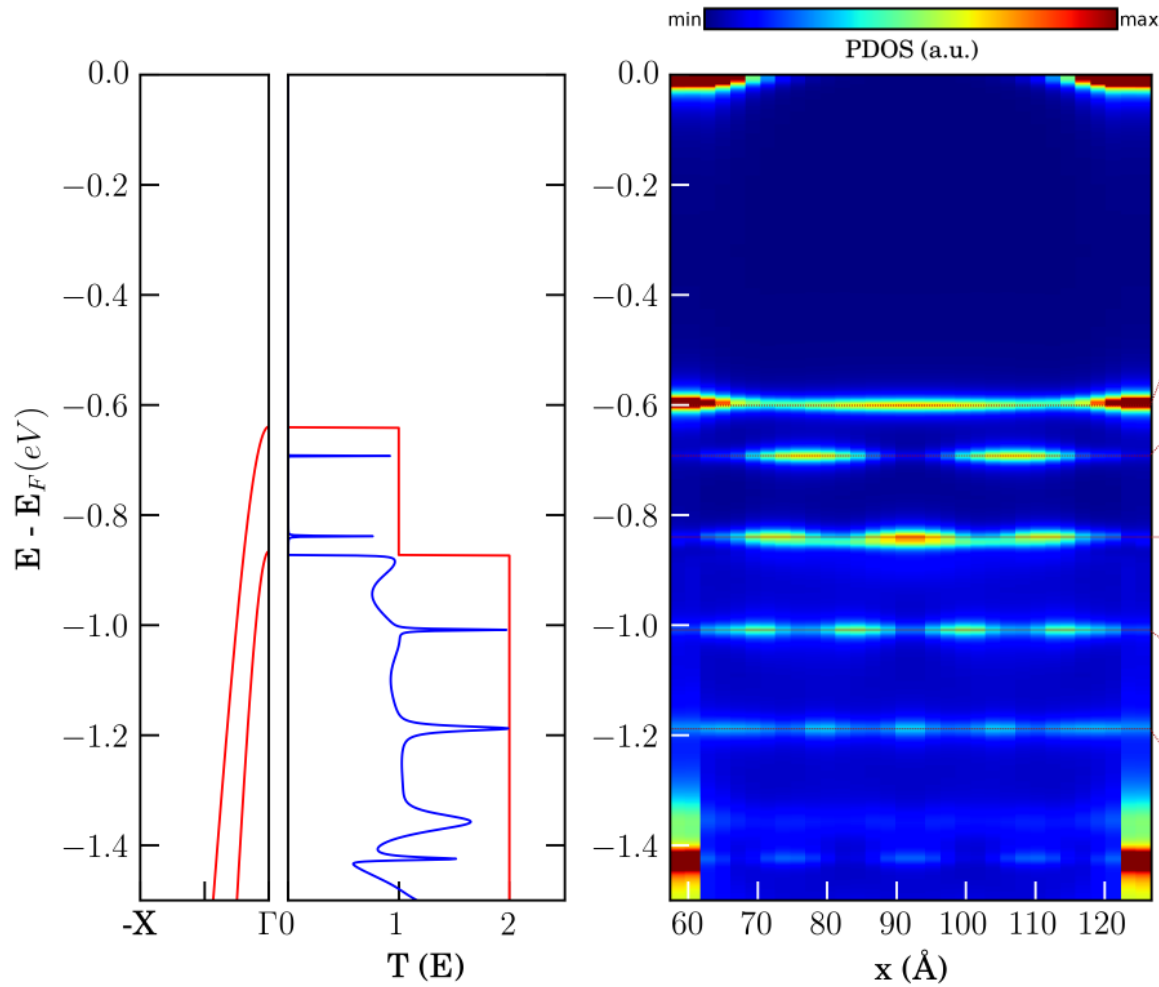
DOS projected on each ribbon “row”



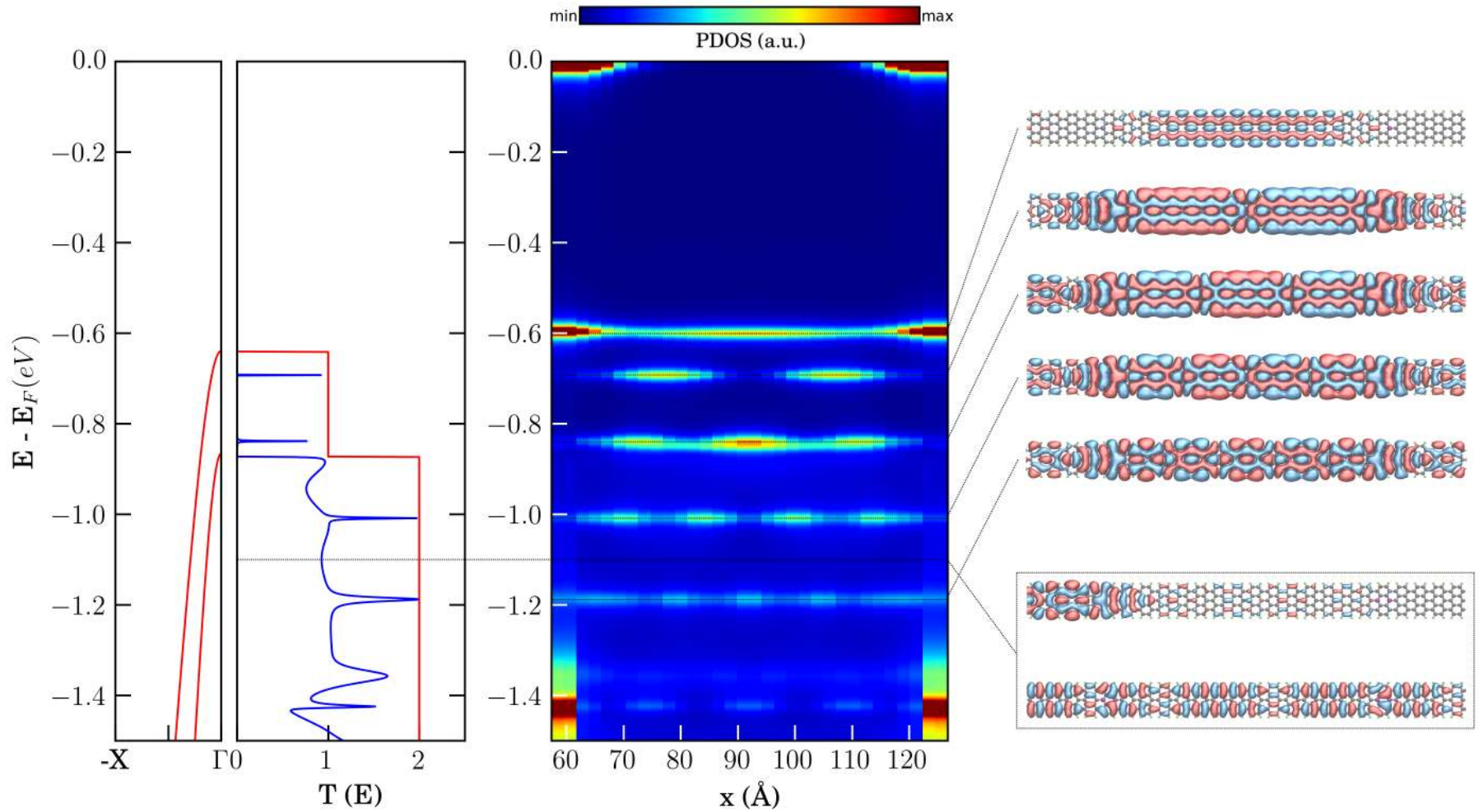
DOS projected on each ribbon "row"



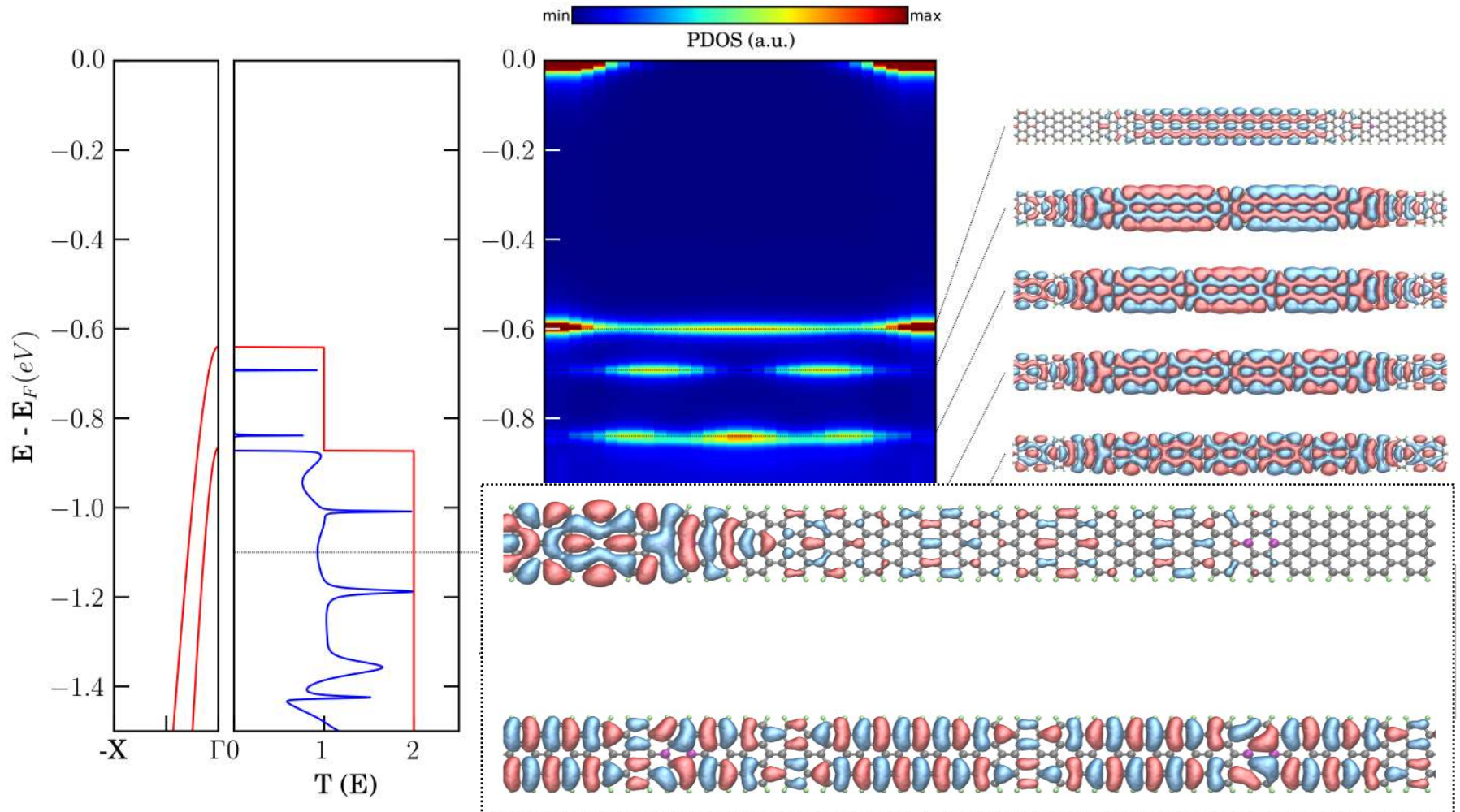
Zero bias transmission



Eigenchannels



Eigenchannels



Conclusions

- Semiconductor electrodes: **use with caution!**
- **Coulomb cutoff in TranSIESTA** for low dimensionality systems;
- Transport simulations can **reproduce** observed quantum well states and **explain** their mechanism.



Thank you!



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